# Engineering Sciences 

OCT 2 '76

Branch Library

WIND FORCES AND MOMENTS
ON
MICROWAVE ANTENNAS
by
Michael Poreh
and
Jack E. Cermak

# A Report to <br> ROSE, CHULKOFF AND ROSE Structural Engineers <br> Sponsored by <br> Long Lines Department <br> AMERICAN TELEPHONE AND TELEGRAPH COMPANY 

Fluid Mechanics and Wind Engineering Program
Department of Civil Engineering
Colorado State University Fort Collins, Colorado 80523

September 1976

## TABLE OF CONTENTS

PAGE
ACKNOWLEDGEMENTS ..... v
INTRODUCTION ..... 1
EXPERIMENTAL CONFIGURATION ..... 4
Wind Tunnel. ..... 4
Model ..... 5
EXPERIMENTAL TECHNIQUES ..... 7
Flow Visualization ..... 7
Measurements of Flow Characteristics ..... 7
Measurements of Forces and Moments ..... 8
PRELIMINARY TESTS. ..... 9
Survey of the Approaching Velocity Field ..... 9
Drag of Platform ..... 10
Reynolds-number Effects. ..... 11
FORCES AND MOMENTS ACTING ON ANTENNA CLUSTERS. ..... 13
Program and Conditions of Tests. ..... 13
Forces Acting on a Single Pyramidal Horn ..... 13
Forces on a Conical Antenna. ..... 14
Forces and Moments on a Two-horn Configuration ..... 16
Forces and Moments on Four-horn Clusters ( 20 ft . Separation) ..... 20
Analysis of "Condition 3A" and "Condition 3B" ..... 24
Experimental Error Analysis ..... 25
A NUMERICAL EXAMPLE ..... 27
SUMMARY. ..... 28
TABLE OF CONTENTS
Continuation
PAGE
FIGURES ..... 30
1 Definition of coordinate system, forces and moments. ..... 31
2 Industrial Aerodynamics Wind Tunnel ..... 32
3 Meteorological Wind Tunnel ..... 33
4 Photograph of model (Condition 3) ..... 34
5 Photograph of plat form ..... 34
6 "Gabriel" conical antenna horn mounted on a single horn plat form ..... 35
7 Photograph of the two-story array. ..... 35
8 Mean velocity and turbulent intensity distribution in the industrial and meteorological wind tunnels during tests. ..... 36
9 Effect of Reynolds number on the drag coefficient (condition 1). ..... 37
10 Effect of Reynolds number on the drag coefficient of single horns ..... 38
11 Drag coefficients of single pyramidal horns ..... 39
12 Drag coefficients of a single conical horn ..... 40
13 Drag coefficients of a two-horn cluster (condition 3C) ..... 41
14 Measured drag on a four horn cluster (condition 1 covered platform) ..... 42
15 Drag coefficients of a four-horn cluster (condition 1 covered platform). ..... 43
16 Drag coefficient of a four horn cluster (condition 1] ..... 44
17 Drag coefficients of a four-horn cluster (condition 3) ..... 45
18 Drag coefficients of a four-horn cluster (condition 3) ..... 46
TABLE OF CONTENTS
Continuation
PAGE
FIGURES (continued)
19 Dependence of the drag coefficient of four-horn clusters on the projected area ..... 47
20 Drag coefficients of a four-horn cluster (condition 3a) ..... 48
21 Measured drag on a four-horn cluster with and without an upper platform. ..... 49
22-39 Schematic view of cluster configuration facing downwind - Condition 3. Wind Directions $0^{\circ}-340^{\circ}$ ..... 50-67
40 Structure of the flow around a four horn cluster "Condition 1", $\theta=180$. ..... 68
41 Structure of flow around a four-horn cluster, "Condition 1" ..... 69
TABLES ..... 70
1 Measured wind forces on model of the $29 \times 29 \mathrm{ft}$ platform ..... 71
2 Effect of Reynolds number on the drag of a four-horn cluster (condition 1 covered platform). ..... 72
3 Summary of tests ..... 73
4 Forces and moments on a single pyramidal horn (with blinders) ..... 74
5 Forces and moments on a single pyramidal horn (without blinders) ..... 75
6 Forces and moments on a single conical horn ..... 76
7 Experimental data for a two-horn cluster (condition 3c) ..... 77
8 Experimental data for a four-horn cluster (condition 1 covered platform) ..... 78
9 Experimental data for a four-horn cluster (condition 1 uncovered platform) ..... 79
TABLE OF CONTENTSContinuation
PAGE
TABLES (continued)
10 Experimental data for a four-horn cluster (condition 2) ..... 80
11 Experimental data for a four-horn cluster (condition 3) ..... 81
12 Experimental data for a four-horn cluster (condition 3A). . ..... 82
13 Experimental data for a four-horn cluster with an upper platform (two story cluster, Condition 3B). ..... 83
APPENDIX ..... 84-94

## ACKNOWLEDGMENTS

The authors gratefully acknowledge the contributions of all those who assisted in carrying out the several phases of this project.

The structure model was fabricated by personnel of the Engineering Research Center Machine Shop. Mr. James A. Garrison carried out the flow visualization program. Mr. Herbert Brauer, Mr. Hiroo Shiojiri and Ms. Janet Floersch accomplished the data acquisition and reduction.

INTRODUCTION
The purpose of this investigation is to obtain quantitative information that will relate the forces and moments acting on a single microwave antenna or on any of several configurations of two- or four-horn antenna clusters to the speed and direction of the approaching wind. The study provides input for a rational design of the towers that support such microwave antenna arrays.

The flow around a single antenna horn or around a cluster of antennas is very complex and defies exact theoretical analysis. The theory indicates, however, that the drag force $D$, the lateral force $L$ and the moments $M_{p}$ and $M_{R}$, as defined in Fig. 1, can be expressed in the following universal forms:

$$
\begin{align*}
& D=C_{D} A \rho U^{2} / 2  \tag{1}\\
& L=C_{L} A \rho U^{2} / 2  \tag{2}\\
& M_{P}=C_{M P} A L \rho U^{2} / 2  \tag{3}\\
& M_{R}=C_{M R} A L \rho U^{2} / 2 \tag{4}
\end{align*}
$$

In these equations $A$ is a reference area; in the present study, unless otherwise stated, $A$ is chosen to be the area of the antennas and platform projected on a plane normal to the wind direction. The length $L$ is a typical (arbitrary) length; in this study we have chosen as a typical prototype length $\mathrm{L}=10 \mathrm{ft}$. The mean wind speed U is taken approximately at the height of the center of mass of the antenna horn or horns as shown in Fig. 8. The mass
density of air near the structure is denoted in the equations by $\rho$. Denoting by $\Delta \mathrm{p}$ the dynamic pressure, $\rho \mathrm{U}^{2} / 2$, as measured by a pitot tube, equations (1), (2), (3) and (4) can also be expressed as follows:

$$
\begin{align*}
D & =C_{D} A \Delta p  \tag{5}\\
L & =C_{L} A \Delta p  \tag{6}\\
M_{P} & =C_{M P} A L \Delta p  \tag{7}\\
M_{R} & =C_{M R} A L \Delta p \tag{8}
\end{align*}
$$

The aerodynamic coefficients $C_{D}, C_{L}, C_{M P}$ and $C_{M R}$, for a specified body and wind orientation, known also as the drag coefficient, the lateral force coefficient and the moment coefficients, respectively, are primarily determined according to theory, by the Reynolds number of the flow which is defined as

$$
\begin{equation*}
\operatorname{Re}=\frac{U L}{V}, \tag{9}
\end{equation*}
$$

where $v$ is the kinematic viscosity of the air. This theory forms the basis for wind tunnel simulation of aerodynamic phenomena in which the values of these coefficients are determined from measurements of the forces and moments acting on small scale models.

Since the aerodynamic coefficients depend primarily on the Reynolds number, these tests should usually be made so that the Reynolds number of the prototype is equal to that of its model. This condition cannot always be met in existing wind tunnels. Fortunately, however, both theoretical considerations and experimental evidence show that beyond a certain critical Reynolds number, there is no significant change in the value of the aerodynamic
coefficients. The value of this critical Reynolds number depends on the geometry of the body and the turbulence level of the air stream.

Therefore, whenever both the prototype Reynolds number and the model Reynolds number exceed the critical value, it is permissible to use the model-derived coefficients as the basis for computation of prototype forces and moments. The regime in which the value of the coefficients remains essentially constant is called the regime of Reynolds Number Independence.

Of course, it is also required that the basic features of the flow field be simulated in the wind-tunnel tests. This requirement is satisfied by testing the models in an approaching flow in which the vertical velocity profile and turbulence characteristics are similar to those of the prototype flow.

The test program for this study was therefore organized as follows:
(a) a survey of the approaching velocity field was performed and recorded;
(b) tests to determine the effect of the Reynolds number were made;
(c) the nature of the flow around specified antenna cluster configurations was studied and recorded using visual techniques; and
(d) measurements of forces and moments in the regime of Reynolds Number Independence were made, and values of the aerodynamic coefficients were determined.

## EXPERIMENTAL CONFIGURATION

## Wind Tunnel

This study was performed in part in the industrial aerodynamics wind tunnel and in part in the meteorological wind tunnel of the Fluid Dynamics and Diffusion Laboratory at Colorado State University.

The industrial aerodynamics wind tunnel is a closed circuit facility driven by a 75 hp variable pitch propeller. The test section is 6 ft by 6 ft and 62 ft long, fed through a 4 to 1 contraction ratio. The roof is adjustable to maintain a zero pressure gradient along the test section. Mean velocity can be adjusted continuously from 1 to 75 fps. A schematic drawing of this tunnel is shown in Fig. 2.

The meteorological wind tunnel is also a closed circuit type with a 6 ft square test section. Its length is 80 ft . Zero pressure gradient is maintained by means of an adjustable roof. Mean velocity can be varied continuously from 1 to 120 fps. A schematic drawing of this tunnel is shown in Fig. 3.

The model was centrally mounted on the turntables in both tunnels as indicated in the figures.

Spire-type vortex generators and a 4 in.-high two dimensional barrier provided a boundary layer trip at the entrance to the test section. The downwind floor of the test section was smooth. This arrangement was designed to provide a boundary layer thickness of approximately 45 in . at the position of the model and a mean velocity profile similar to that for a rural environment.

Model
To obtain accurate measurements of mean forces and moments on a structure, a model is usually constructed to the largest scale that will not produce serious blockage in the wind tunnel. In this study, a $1: 16$ scaled model of the upper portion of the support tower, the platform, and the antenna array was constructed to prototype specifications supplied by the sponsors. (See Appendix) The cross section area of the model was at most $5 \%$ of the wind-tunnel cross section. A photograph of the model is shown in Fig. 4.

The upper portion of the support tower was modelled in steel so that all significant particulars of the prototype were represented.

The platform was modelled using $1 / 2 \mathrm{in}$. high steel bars, in such a way as to permit mounting of the antenna horns in specified configurations. An upper view of the platform is shown in Fig. 5. The prototype platform dimensions were $29 \mathrm{ft} \times 29 \mathrm{ft}$. The space in which the antenna horns were installed corresponds to an $8 \mathrm{ft-8} \mathrm{in}$. $\mathrm{x} 8 \mathrm{ft}-8 \mathrm{in}$. square in the prototype.

This platform model was not directly attached to the tower model, but was connected to the force balance which in turn was fastened to the tower.

To simulate an effectively solid-surfaced platform, caused in nature by icing of the platform grating, a cardboard overlay covering the top of the model platform was used. The space required by the prototype specifications to accomodate mounting of each antenna horn ( $7 \mathrm{ft} \times 7 \mathrm{ft}$ ) was left uncovered.

A separate platform model for single antenna horn configurations was constructed of $1 / 2 \times 63 / 4 \times 103 / 4$ in. steel plate, as shown in Fig. 6.

The pyramidal antenna horn models were fabricated of "Lucite" in the Engineering Research Center shop. The "Gabriel" conical antenna-horn model built to a scale of $1: 16$ (see Fig. 6) was supplied by the sponsor. Hereafter the pyramidal antenna horns are referred to simply as "antennas." The "Gabriel" conical antenna horn is called the "conical antenna."

The four pyramidal antenna-horn models were attached directly to the model platform to represent accurately the several prototype configurations specified by the sponsors as given in the appendix. Fig. 4 is a photograph of the antennas mounted in "Condition 3."

In addition, tests were run in a configuration involving a two-story antenna array, as shown in Fig. 7. For this case, the lower story configuration was assembled as in "condition 3." The upper platform in this case was modelled of $1 / 2 \mathrm{in}$. solid plywood plate with four antenna horns made of styrofoam. These horns were mounted in a 16 ft prototype separation configuration. The plane of the upper platform was parallel to the plane of the lower platform. The vertical separation of platforms in the model corresponded to a prototype separation of 15 ft . The principal axes in the plane of the upper platform were oriented at an angle of 45 degrees with respect to the principal axes in the plane of the lower platform.

To damp the excess vibration of the multiple antenna-platform assembly, two dashpots, shown in Fig. 7, were installed on the model. The cylinders containing viscous fluid were attached to the tower portion of the model. The pistons were attached to the platform-antenna assembly in such a way that they did not discernibly contribute to the forces or moments acting on the platformantenna assembly.

## EXPERIMENTAL TECHNIQUES

## Flow Visualization

Visualization of the flow in the vicinity of the model is helpful in understanding and interpreting the mean force and moment measurements. Titanium tetrachloride smoke was released from upstream sources close to the model. Motion and still-picture records of the flow patterns were taken and constitute a part of the final report to the sponsor. Selected photographs appear in Fig. 40-.

Measurements of Flow Characteristics
Velocity and turbulence intensity profiles of the flow under test conditions were made at the locations of the model (turntables) in the two tunnels with the model removed. The integral scale of the longitudinal component of turbulence at the height of the center of mass of the antennas was also determined. Results of these measurements will be discussed later in the report.

The measurements were made with a single hot-wire anemometer. The instrumentation used was a Thermo-Systems constant-temperature anemometer (Model 1050) with a 0.001 in.-diameter platinum film sensing element 0.020 in. long. Output was read from a Hewlett-Packard integrated digital voltmeter (Model 2401C) for mean voltage and a DISA rms meter (Model 55D35) for rms. voltage.

The reference velocity was obtained by using a standard Pitot tube. The dynamic pressure $\Delta \mathrm{p}$ was recorded by a Baratron Pressure Gage in mm of mercury.

Measurements of Forces and Moments


#### Abstract

Mean force and moment measurements were made using a strain-gauge instrumented force balance manufactured by Inca Engineering Corporation of San Gabriel, California. This balance can measure all six components of forces and moments, although the sensitivity to forces along the balance axis is too low for the accuracy desired. For this reason the balance was aligned with its axis in a vertical position for measurement of horizontal forces and moments.


## PRELIMINARY TESTS

## Survey of the Approaching Velocity Field

The flow field at the locations of the model was surveyed. The mean velocity profile in both tunnels exhibit similarity in the sense that variation of the ratio of the local mean velocity in the boundary layer to the mean velocity outside the boundary layer $U(z) / U(\infty)$ is independent of the value of $U(\infty)$ as shown in Fig. 8. The boundary layer thickness was also the same in both tunnels and is estimated to be $\delta=45 \mathrm{in}$. The primary reason for obtaining the same boundary-layer thickness, in spite of the slight difference in the length of the test sections, is that $\delta$ was primarily determined by the vortex generaters and trip fence used to augment the thickness of the boundary layer at the entrances to the tunnels.

The height of the tower was such that the top of the platform was located at the height of 34 in. from the floor of the tunnel and the estimated center of pressure of the horn's surface was at 38 in. from the floor, as shown in Fig. 8. As seen from this figure the variation of the approaching velocity across the horns was very small, of the order of a few percent. The reference velocity $U$ in subsequent tests was taken as the velocity at 38 in. from the floor measured upstream from the model.

The distribution of the turbulence intensity in the tunnels is also shown in Fig. 8. At the height of the horns it varied between 4 to 5 percent.

The measured characteristics of the flow field appear to be similar to the average characteristics of the atmospheric boundary layer as discussed by Cermak*. It should be stressed, however, that the existing force and

[^0]moment measurements are average values and do not contain the gust loading. Thus, it is recommended that the peak forces and moments for gust loading be obtained by using Equations (1) - (4) with $U$ replaced by the estimated gust velocity.

## Drag of Platform

Preliminary tests were conducted to determine the drag of the fourhorn platform (Fig. 5) and to find the possible effect of platform inclination due to wind forces in the tests. It should be noted that during the tests the platform and horns were connected to the elastic balance. The maximum inclination of the platform during the tests was estimated to be smaller than $1 / 2$ degrees. The effect of such an inclination on the drag of the horns is expected to be very small; however, it was not clear whether the relatively large change in the projected area of the inclined platform would increase the drag. The platform's drag was therefore measured at two orientations of its principal axes, 0 and 45 degrees, at 0,2 and 4 degree inclinations. The data are given in Table 1 .

The results clearly show that the effect of $1 / 2$ degree inclination of the platform is negligible. The value of the drag coefficient of the uncovered platform at 0 degree orientation was found to be very high $C_{D}=5.88$. Usually a value of $C_{D}=2$ is expected for a bar oriented normal to the flow and $C_{D}=1$ for a solid short plate. In this case, however, the platform is made of several parallel bars. Although the downstream bars do not change the projected area, a considerable aerodynamic force is exerted on them to produce a large value of the drag coefficient. When oriented at 45 degrees, the drag coefficient of the platform goes down to $C_{D}=3.7$. Note that the total ratio of the horizontal area of the platform to the projected area is decreased, by 1.4 .

No correction was made in the tests for drag increase due to effects of the supporting elements which connected the platform to the balance. It is estimated that the supporting elements increased the drag of the platform by approximately $15 \%$. The effect of these elements on the total drag of the antenna horns and platform is, however, one order of magnitude smaller.

A comparison between the drag of the covered platform and that of the uncovered platform, given in Table 1, clearly shows, as expected, that the drag of the uncovered platform is slightly higher.

The drag of the platform used for the single-horn tests was even smaller but so was the drag on the horns. In this case it was estimated that the wake of the horn reduced the platform's drag by 50 percent. This estimate was made by measuring the drag on the platform with the horn held in its place without touching the platform. The data were corrected accordingly and the drag of single horns as discussed later is the net drag of the horns.

## Reynolds-number Effects

Tests were conducted to examine the effect of the Reynolds number on the drag coefficient and to determine the lower bound of the Reynolds Number Independence regime.

The horns were mounted on the platform in "Condition 1" (See Appendix) and the drag was measured for four wind directions at five Reynolds numbers ranging from $1.1 \times 10^{5}$ to $3.2 \times 10^{5}$, which correspond to speeds of 33 and $100 \mathrm{ft} / \mathrm{sec}$. (Note that the Reynolds number was calculated using Equation 9 with $\mathrm{L}=0.625 \mathrm{ft}$ which correspond to $\mathrm{L}=10 \mathrm{ft}$ in the prototype.) The corresponding drag coefficients are given in Table 2 and plotted in Fig. 9.

It is clear from the results that beyond $R e \cong 2.5 \times 10^{5}$ or $V=70 \mathrm{ft} / \mathrm{sec}$ no Reynolds number effect is detected. It was therefore decided to continue the tests at a speed of approximately $70 \mathrm{ft} / \mathrm{sec}\left(48 \mathrm{mi} / \mathrm{hr}\right.$ ) where $C_{D}$ is not a function of the Reynolds number and where the effect of inclination and model vibrations are small.

Similar tests were conducted with a single pyramidal horn and with a single conical horn. The results of these tests are shown in Fig. 10. The scatter here is slightly larger due to the smaller magnitude of the drag. The data do not, however, show a clear Reynolds number dependence. The single horn tests were conducted at a velocity of approximately $U=84 \mathrm{ft} / \mathrm{sec}$. (Note that the velocity in $\mathrm{ft} / \mathrm{sec}$ equals approximately $54 \sqrt{\Delta \mathrm{p}}$ where $\Delta \mathrm{p}$ is expressed in mm of mercury. The coefficient 54 depends on the density of the air at the altitude where the velocity is measured.)

## FORCES AND MOMENTS ACTING ON ANTENNA CLUSTERS

Program and Conditions of Tests
The forces and moments defined in Fig. 1 have been measured on a single (pyramidal) horn, a conical horn, a two-horn cluster, and various configurations of four-horn clusters. A summary of the testing program is given in Table 3. The exact orientation of the horns, the separation between the horns and the projected areas of the cluster in each configuration and wind orientation are given in the Appendix.

The drag, lateral force and moment coefficients were calculated using Equations (5) to (8). The height of the drag force $y_{D}$ was calculated using the ratio of the pitching moment to the drag force:

$$
\begin{equation*}
y_{D}=\frac{M_{P}}{D} \tag{10}
\end{equation*}
$$

Forces Acting on a Single Pyramidal Horn
The forces, moments and calculated values of the aerodynamic coefficients of a single pyramidal horn are given in Tables 4 and 5.

It should be pointed out again that the absolute magnitudes of the lateral forces and moments recorded in this case were small compared to the full-scale range of the balance. This reduced the accuracy of the singlehorn measurements relative to the multiple-horn data. Nevertheless, inspection of the recorded data clearly indicates the lateral forces are usually very small compared to the drag forces. Only at orientations between $20^{\circ}$ and $60^{\circ}$ was the lateral force coefficient significant, but even in these cases its value was less than $30 \%$ of the drag coefficient. The resultant force

$$
F=\left(D^{2}+L^{2}\right)^{1 / 2}
$$

would therefore be at most $5 \%$ larger than the drag force. This finding, as we shall see later, is also typical of the two- and four-horn configurations and it clearly indicates that the significance of the lateral forces is relatively small. The roll moment was also found to be very small and relatively insignificant.

The values of the drag coefficients at different wind orientations are plotted in Fig. 11. The maximum value of the drag coefficient,

$$
C_{D}=1.31,
$$

was recorded when the horn was facing the wind, $\theta=0$. In the range $20^{\circ}<\theta \leq 90^{\circ}$ the value of the drag coefficient varied between $1.0<\mathrm{C}_{\mathrm{D}}<1.2$. On the other hand, when the antenna faced the downstream direction, $90<\theta \leq 180$, the drag coefficient was about $20 \%$ lower and varied between $0.8<\mathrm{C}_{\mathrm{D}}<1.0$.

The removal of the blinders (mark $\AA$ in Fig. Al of the appendix) decreased the drag coefficient by approximately $10 \%$ in the cases where the angle of incidence between the blinder and the wind was 30 to 90 degrees. Forces on a Conical Antenna

The data for the single conical "Gabriel" type antenna are given in Table 6. In this case too, the absolute magnitudes and relative significance of the lateral forces and the rolling moments were small. (In one case a ratio of $C_{L} / D_{D}=1 / 3$ was recorded but in this case the relative magnitude of $C_{D}$ was also small).

The variation of the drag coefficient is plotted in Fig. 12. A maximum value of

$$
C_{D}=0.89
$$

was obtained when the antenna was facing the wind, $\theta=0$. In the other orientations the value of the drag coefficient varied between $C_{D}=0.51$, when oriented at a right angle to the wind, and $C_{D}=0.8$. The relatively low value of $C_{D}$ in the $\theta=90^{\circ}$ orientation is not surprising as the upper shape of the antenna has a form of a cylinder which has a rather low drag coefficient.

Forces and Moments on a Two-horn Configuration
Although the tests of the two-horn configuration were performed at the end of the program, it is instructive to analyze the results of these tests before those of the four-horn configuration. The data of the tests are given in Table 7 and the variation of the drag coefficient is plotted in Fig. 13.

As seen from this figure the drag coefficient in this configuration varies from a minimum of $C_{D}=1.15$ to a maximum of $C_{D}=1.65$. Let us first examine the values of the drag coefficients for the range $60^{\circ} \leq \theta \leq 120^{\circ}$. In this range there is only a slight interaction between the two horns. This claim is also supported by the visual observations of the flow pattern which have been recorded in a motion picture. (Still photographs of the flow pattern in several cases are given in Figs 40- . The quality of these is not very high because of the long time of exposure. They do show, however, the structure of the wake behind the horns and the complex flow pattern due to the interaction between the wake and the back horns). In Figs. 22-39 we have plotted schematic views of the clusters in "Condition 3", as seen by an observer looking down wind. Our case, Condition 3C, is slightly different as the separation between the horns is 16 ft and only horns (1) and (2) are mounted on the platform. Nevertheless the general view of the configuration 3C in the range $60 \leq \theta \leq 120$ is apparent from Figs. 26 to 28 . In the case $\theta=60^{\circ}$ we find, for example, that both horns face the wind with their backs. Let us try to estimate the drag of this configuration.

Horn No. 1 is at an angle of $110^{\circ}$ with respect to the wind and horn No. 2 is at an angle of $135^{\circ}$ to the wind. According to Table 1 the drag
coefficient of the platform is approximately 4. The corresponding areas of the two horns and the platform are 116,141 and $25 \mathrm{ft}^{2}$. The total projected area is actually only 276 because of some shading. Thus the total drag coefficient should be

$$
C_{D} \sim \frac{0.80 \times 116+0.85 \times 141+4.0 \times 25}{276}=1.13 .
$$

The measured drag coefficient was

$$
C_{D}=1.21 .
$$

When the two horns face the wind as in the orientation $\theta=240^{\circ}$ and $\theta=260^{\circ}$ the individual drag coefficients go up as shown in Fig. 11, which causes the total drag to increase to approximately

$$
C_{D}=1.47
$$

Such calculations are of course not very reliable since they neglect the interaction between the various elements of the cluster. However, they do give a partial explanation for the variation of $C_{D}$. They fail completely when the horns are close to each other and when one horn is partially located in the wake of another horn as in the cases $\theta=0$ and $\theta=180$. In these cases the projected areas are drastically reduced, however, the force acting on the shaded sections of the back horn are not zero. This increases the drag coefficient considerably. Indeed, one finds for $\theta=0$ $C_{D}=1.65$, and for $\theta=180^{\circ} C_{D}=1.52$.

The case of $\theta=340^{\circ}$ where $C_{D}$ reaches a minimum is more difficult to explain. One possible explanation is that although the back horn is hardly shaded by the front one, the force on the back horn is reduced due to the wake.

It should be noted that although the drag coefficient is maximum at $\theta=0$, the largest force on the structure is exerted when $\theta=260^{\circ}$. In this case the projected area has its maximum and the drag coefficient is also high as both horns face the wind.

Let us examine now the variation of the roll moment coefficient denoted in Table 7 by $C_{M R}$. Its absolute value has maximums at $\theta=0$ and $\theta=180$. Indeed in these orientations the two horns are on one side of the platform. The value of $\mathrm{C}_{\mathrm{MR}}$ for these cases can be estimated using the following approximations:

$$
M_{R} \sim D \cdot \ell \cdot \alpha
$$

where $\ell$ is approximately half the separation ( 8 ft ) and $\alpha$ is the portion of the drag force which acts on the horns. (About $30 \%$ of the drag, which acts on the platform, does not create a moment.) Since $D=C_{D} A \rho U^{2} / 2$ and $M_{R}=C_{M R} A \cdot L \rho U^{2} / 2(L=10 \mathrm{ft})$, one gets

$$
C_{M R} \sim C_{D} \cdot \ell / L \cdot \alpha=0.92
$$

which is very close to the measured value. Of course such calculations can usually yield only a rough estimate.

Estimates of the pitching moment become more difficult. Obviously the pitching moment should always be positive since the resultant drag force acts at a height $y_{D}$ above the level of the platform. The measured values of $y_{D}$ varied from $y_{D}=1.6$ to $y_{D}=5.6$. The variations in the height of $y_{D}$ is primarily due to the shift of the center of pressure of
the projected area of the cluster. When a horn is facing the wind the center of pressure is high, and when a horn is facing the side ( $\theta \sim 90^{\circ}$ ) it goes down. The relative magnitude of the force on the platform has also an effect on the position of $y_{D}$. (It should be stressed that when the absolute value of the moments become small as in the $80^{\circ}$ orientation the accuracy of our $y_{D}$ measurements is decreased.

The magnitude of the lateral forces acting on the two-horn cluster is relatively very small, around $20 \%$ of the drag force. This is equivalent to an increase of only $2 \%$ in the magnitude of the total force $F$, defined in Eq. 10.

Forces and Moments on Four-horn Clusters (20 ft. Separation)
We have tested the wind effects on three configurations of four-horn clusters with a 20 ft separation between neighboring horns. We have then tested one four-horn configuration with 16 ft separation and the effect of an upper platform with four horns on the drag of a lower platform.

Tables 8 and 9, as well as figs. 14 to 16 , show the data for Condition 1 , with a covered and with an uncovered platform. The drag coefficients varied in this condition between 1.0 and 1.63 for the cluster with the covered platform and between 1.1 to 1.67 for the uncovered platform. Since the projected area of the platform in clusters of four horns is relatively small, of the order of $5 \%$, the relative effect of covering the platform was rather small although it is clear that it has in most cases a positive effect and the covering of the platform reduced the drag. It should be stressed, however, that the covering in our model was relatively smooth and has hardly increased the projected area.

In examining the variation of the drag coefficient, one should distinguish between three cases. When the cluster is at $0^{\circ}$ and $180^{\circ}$ orientation with respect to the wind, the back horns are largely hidden behind the front ones. In these cases the projected area goes considerably down but since some force is exerted on the back horns the drag coefficient goes up to about

$$
C_{D}=1.7
$$

Around $\theta=45^{\circ}, 135^{\circ}, 225^{\circ}$ and $315^{\circ}$ only one of the horns is shaded. Indeed, the drag coefficient graph showed a small maximum in the neighborhood of these
angles and values around

$$
C_{D}=1.4
$$

were recorded. When the horns on the back are not shaded, the drag coefficient goes down to values around

$$
C_{D}=1.2 .
$$

Similar results were obtained for "Condition 2" and "Condition 3". The data for these cases is tabulated and plotted in Tables 10 and 11 and Figs. 17 and 18. The maximum drag coefficient was recorded a $\theta=0$ for "Condition 2"

$$
C_{D}=1.9
$$

It is noted that at $\theta=0$ the shading of the back horns was the largest and the projected area was the smallest. This case does not give, however, the maximum drag, which had been recorded in "Condition 3" at an angle of $\theta=300^{\circ}$ when the projected area was $518.5 \mathrm{ft}^{2}$.

Obviously only a very rough estimate of the drag coefficient in such a complex configuration can be made. It was therefore decided to examine the entire set of data in order to look for the general dependence of $C_{D}$ on the projected area. Figure 19 shows all the data plotted versus the prototype area A.

The figure clearly suggests that both the average and the maximum values of the drag coefficient, for a given value of $A$, decrease as the value of $A$
decreases, although large variations of $\pm 20 \%$ at each value of the projected area exist. The upper bound of the data is approximately described by the equation

$$
\begin{equation*}
C_{D}=2.0\left(\frac{\text { Area }\left(\mathrm{ft}^{2}\right)}{250}\right)-0.5 \tag{11}
\end{equation*}
$$

which results in a drag which is proportional to the square root of the area.

It is noted that in this $\log -\log$ plot a line of constant drag is described by a curve $C_{D} \propto A^{-1}$ which correspond to a line with a slope 1:1. The line of constant drag which passes through the point which corresponds to $\theta=300$, Condition 3 , is shown in this curve by a dashed line.

Although it is difficult to fully explain why $C_{D}$ varied considerably at the same projected area, a partial explanation is sometimes possible. Consider the two points in Fig. 19 which correspond to $A \simeq 426$ sq. ft. (Condition 3, $\theta=80^{\circ}$ and $260^{\circ}$ ). The two cases are described in Figs. 26 and 30.

It is obvious from Fig. 26 that in the case $\theta=80^{\circ}$ all the four horns are oriented with their back to the wind. We have seen earlier that a lower drag coefficient result for such an orientation. It is not surprising therefore that a value of $C_{D}=1.15$ was recorded here compared to a value of $C_{D}=1.43$ at $\theta=260^{\circ}$.

The lateral force coefficients for all three conditions, as well as the roll-moment coefficients, were found to be relatively small.

The position of the drag force above the platform for four-horn clusters varied in the range

$$
3.0 \mathrm{ft}<\mathrm{y}_{\mathrm{D}} \leq 7.6 \mathrm{ft} .
$$

The largest value recorded was at $\theta=0$ for the covered platform. In this case the center of pressure of the horn was high and the force on the platform was relatively low.

Analysis of "Condition 3A" and "Condition 3B"
In Condition 3 A we have tested the effect of decreasing the separation between neighboring horns to 16 ft . In comparing "Condition 3 A " to "Condition $3^{\prime \prime}$ it is found that the drag coefficients have in general been decreased by approximately $10 \%$. Taking into consideration the slight difference in the stagnation pressure between the two experiments it can be shown that the maximum drag had also decreased by $10 \%$.

The effect of an upper platform, shown in Fig. 21, has also been to reduce the drag but not uniformly. Unfortunately the data points corresponding to $\theta=240^{\circ}$ and $260^{\circ}$ were found to be in error and were omitted. It is also noted that the maximum drag appeared at a slightly different angle and its value was $16 \%$ smaller.

Both Condition $3 A$ and $3 B$ suggest that a compact arrangement of the horns would reduce the drag of the cluster.

## Experimental Error Analysis

One should distinguish between errors in the experimental evaluation of the drag coefficient for the models and possible deviation of drag coefficients for the prototypes from those of the models.

The balance and electronic system are supported by their specification to be accurate within $0.1 \%$ of full scale. Our experience is, however, that a $0.4 \%$ error is a more realistic value. The full scale of the balance is 50 lbs which gives an error of 0.2 lbs . This would mean a possible error of $\pm 2 \%$ error in the drag measurements of the four-horn clusters, a $\pm 4 \%$ in the two-horn clusters and a possible $\pm 8 \%$ error in the single horn experiments.

The error in the stagnation pressure measurement is estimated to be of the order of $\pm 2 \%$. Now, the authors had not noticed before the experimental work was completed that the configuration of the cluster in "Condition $2^{\prime \prime}$ is symmetric about one of the axes. Thus, we have measured 12 pairs of data points which should ideally give the same drag coefficients. Denoting the two readings of each pair by $\mathrm{a}_{\mathrm{i}}$ and $\mathrm{b}_{\mathrm{i}}$ we have calculated the average value $m_{i}=\left(a_{i}+b_{i}\right) / 2$ and the deviation $d_{i}=\left|a_{i} / m_{i}-1.0\right|$ for each pair. A maximum deviation of $d_{i}=0.04$ was recorded but the average value of $d_{i}$ was 0.02. This is consistent without previous estimates of the possible error. It is therefore suggested that standard deviation of the errors for the four-horn cluster measurements is approximately $3 \%$.

The errors for the single horn measurements and the lateral forces are of course larger by a factor of 3 . Another effect which has been neglected is that of the blockage. It is estimated that the blockage has increased
the measured values of the drag coefficient by approximately 2-4\%. No correction has however been made for this effect.

Theoretically, the values of the prototype coefficients should be equal to those of the model. However, the standard deviation of the prototype data would probably be much larger than in the model. In particular one should recall that the accuracy of estimating the wind velocity in nature is not very high and that the forces are proportional to the square of the velocity.

One may thus conclude that the experimental errors in this study are relatively small and the values proposed could be used for design of the supporting tower provided an acceptable estimate of the wind velocity and gust level is available.

## A NUMERICAL EXAMPLE

Calculate the maximum drag acting on a four-horn antenna configuration in "Condition 3 " when the wind speed is $100 \mathrm{mi} / \mathrm{hour}$ ( $146.7 \mathrm{ft} / \mathrm{sec}$ ). According to Table 11 the maximum drag occurs at $\theta=300^{\circ}$. The projected area at this orientation is $A=518.5 \mathrm{sq}$. ft . The drag coefficient is $C_{D}=1.33$.

Assuming that the tower is located at sea-level the density of the air is assumed to be

$$
\rho=0.127 \mathrm{kgf}-\mathrm{sec}^{2} / \mathrm{m}^{4}=0.00242 \mathrm{slug} / \mathrm{ft}^{3}
$$

giving a dynamic pressure

$$
\Delta \mathrm{p}=\frac{\rho \mathrm{U}^{2}}{2}=26.03 \quad \mathrm{lbs} / \mathrm{ft}^{2}
$$

The total drag according to Eq. 5 would thus be

$$
D=C_{D} \Delta p \cdot A=(1.33)(26.03)(518.5)=17950 \mathrm{lbs}
$$

The position of the drag force will be at

$$
y_{D}=5.3 \mathrm{ft} .
$$

above the platform.
The lateral force and roll moment in this case are practically zero.

SUMMARY
Mean wind forces and moments acting on $1: 16$ scale models of various microwave antenna cluster configurations were measured in a wind tunnel. Aerodynamic force and moment coefficients for the Reynolds Number Independence Regime were determined.

The drag coefficient of a single pyramidal horn was found to vary in the range

$$
0.8 \leq C_{D} \leq 1.3 .
$$

Values larger than $C_{D}=1.0$ were obtained when the horn was facing the wind $0 \leq \theta \leq 90^{\circ}$, whereas values of $C_{D}<1.0$ were always recorded when the horn was facing the downwind direction, $90^{\circ}<\theta \leq 180^{\circ}$.

The drag coefficient of the "Gabriel" conical horn was usually $30 \%$ lower than that of the pyramidal horn and varied in the range

$$
0.5<C_{D}<0.9
$$

The drag coefficient of the platform used to support four-horn clusters was found to be relatively very large, particularly when the platform was not covered. In one case the large number of steel bars located in the wake increased the drag coefficient of the platform up to

$$
C_{D}=5.9 .
$$

The experiments have also indicated that the effect of a vertical wind component would be to further increase the drag of the platform.

The drag coefficient of two- and four-horn configurations which included the platform was found to vary in the range

$$
1.0<C_{D}<1.9 .
$$

The average value of $C_{D}$ appears to be inversely proportional to the square root of the projected area giving a total drag which increases as the square root of the projected area. Its value for a given projected area is apparently affected by the orientation of the individual horns and was usually high when all four horns were facing the wind. Also note that the maximum drag does not occur at the orientation where $C_{D}$ is maximum.

A compact cluster configuration, due to a small separation between the horns or a two-story configuration usually reduced the drag coefficients.

The lateral forces acting on the cluster normal to the wind direction were found to be generally small. The vectorially combined force of the drag and lateral force was at most $5 \%$ higher than the drag force alone. The roll moment was found to be insignificant in case of four-horn clusters but was large in case of two-horn clusters.

$z \quad$ vertical axis
D drag force
L lateral force
$\mathrm{M}_{\mathrm{R}} \quad$ rolling moment
$M_{P}$ pitching moment
$y_{D}$ height above platform of drag force ( $y_{D}=M_{P} / D$ )
$\theta$ angle defining wind orientation
$a-c, b-d \quad$ principal axes of platform

Fig. 1 Definition of coordinate system, forces and moments


ELEVATION

Fig. 2 INDUSTRIAL AERODYNAMICS WIND TUNNEL
FLUID DYNAMICS \& DIFFUSION LABORATORY COLORADO STATE UNIVERSITY



Fig. 3 METEOROLOGICAL WIND TUNNEL (Completed in 1963)
FLUID DYNAMICS \& DIFFUSION LABORATORY
COLORADO STATE UNIVERSITY


Fig. 4 Photograph of model (Condition 3).


Fig. 5 Photograph of plat form.


Fig. 6 "Gabriel" conical antenna horn mounted on a single horn platform


Fig. 7 Photograph of the two story array. (The viscous dash pots are shown in front of the model.)


Fig. 8 Mean velocity and turbulent intensity distribution in the industrial and meteorological wind tunnels during tests.

Reynolds Number


Fig. 9 Effect of Reynolds number on the drag coefficient (condition 1)

Reynolds Number


Fig. 10 Effect of Reynolds number on the drag coefficient of single horns


Fig. 11 Drag coefficients of single pyramidal horns


Fig. 12 Drag coefficients of a single conical horn


Fig. 13 Drag coefficients of a two-horn cluster (condition $3 C$ )


Fig. 14 Measured drag on a four horn cluster (condition 1 covered platform)


Fig. 15 Drag coefficients of a four-horn cluster (condition 1 covered platform)


Fig. 16 Drag coefficient of a four horn cluster, condition 1


Fig. 17 Drag coefficients of a four-horn cluster (condition 3)


Fig. 18 Drag coefficients of a four-horn cluster (condition 3)


Fig. 19 Dependence of the drag coefficient of four-horn clusters on the projected area


Fig. 20 Drag coefficients of a four-horn cluster (condition 3a)


Fig. 21 Measured drag on a four-horn cluster with and without an upper platform


## Condition 3

Wind Direction $0^{\circ}$
$C_{D}=1.71$
(uncovered platform).


Fig. 22 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $0^{\circ}$.


## Condition 3

Wind Direction $20^{\circ}$
$C_{D}=1.17$
(uncovered platform).
(uncovered platform).


Fig. 23 Schematic view of cluster configuration facing downindCondition 3. Wind Direction $20^{\circ}$.


Fig. 24 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $40^{\circ}$.


Fig. 25 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $60^{\circ}$.


Condition 3
Wind Direction So ${ }^{\circ}$
$C_{D}=1.14$
(uncovered platform).


Fig. 26 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $80^{\circ}$.


## Condition 3

Wind Direction $100^{\circ}$
$C_{D}=127$
(uncovered platform).


Fig. 27 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $100^{\circ}$.


Fig. 28 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $120^{\circ}$.


Condition 3
Wind Direction $140^{\circ}$
$C_{D}=1.27$
(uncovered platform).


Fig. 29 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $140^{\circ}$.


## Condition 3

Wind Direction $160^{\circ}$
$C_{D}=1.13$
(uncovered platform).


Fig. 30 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $160^{\circ}$.


## Condition 3

Wind Direction $180^{\circ}$
$C_{D}=1.57$
(uncovered platform).


Fig. 31 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $180^{\circ}$.


Fig. 32 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $200^{\circ}$.


## Condition 3

Wind Direction $220^{\circ}$
$C_{D}=1.56$
(uncovered platform).


Fig. 33 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $220^{\circ}$.


Condition 3
Wind Direction $240^{\circ}$
$C_{D}=1.29$
(uncovered platform).


Fig. 34 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $240^{\circ}$.


## Condition 3

Wind Direction $260^{\circ}$
$C_{D}=1.43$
(uncovered platform).


Fig. 35 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $260^{\circ}$.


Fig. 36 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $280^{\circ}$.




Fig. 38 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $320^{\circ}$.


> Condition 3
> Wind Direction $340^{\circ}$
> $C_{D}=1.08$
> (uncovered platform).


Fig. 39 Schematic view of cluster configuration facing downwindCondition 3. Wind Direction $340^{\circ}$.

a. Smoke filaments exhibit the structure of the flow.
b. Smoke released from a point source shows that the downstream horn is submerged in the wake of the front horn.


Fig. 40 Structure of the flow around a four horn cluster "Condition 1 ", $\theta=180$. Direction of wind from top to bottom of page.


$$
\theta=220^{\circ}
$$



$$
\theta=240^{\circ}
$$



$$
\theta=300^{\circ}
$$

Fig. 41 Structure of flow around a four-horn cluster, "Condition 1". (Wind direction from top to bottom of page)

TABLES

| PLATFORM | ANGLE OF INCLINATION $\beta$ (deg) | WIND DIRECTION $\theta$ (deg) | PROJECTED AREA OF PLATFQRM A ( $\mathrm{ft}{ }^{2}$ ) | $\Delta \mathrm{p}$ | DRAG <br> (lbs) | $\mathrm{C}_{\text {D }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| uncovered | 0 | 0 | 19.3 | 1.67 | 2.07 | 5.88 |
| " | 0 | 45 | 27.3 | 1.67 | 1.85 | 3.72 |
| " | 2 | 0 | 19.3 | 1.67 | 1.96 | 5.58 |
| " | 2 | 45 | 27.3 | 1.67 | 1.90 | 3.83 |
| " | 4 | 0 | 19.3 | 1.67 | 2.59 | 7.36 |
| " | 4 | 45 | 27.3 | 1.67 | 2.34 | 4.70 |
| covered | 0 | 0 | 19.3 | 1.67 | 1.71 | 4.86 |
| " | 0 | 45 | 27.3 | 1.67 | 1.19 | 2.40 |
| " | 2 | 0 | 19.3 | 1.67 | 1.49 | 4.25 |
| " | 2 | 45 | 27.3 | 1.67 | 1.58 | 3.19 |
| " | 4 | 0 | 19.3 | 1.67 | 2.45 | 6.97 |
| " | 4 | 45 | 27.3 | 1.67 | 2.12 | 4.26 |



Table 1. Measured wind forces on model of the $29 \times 29 \mathrm{ft}$ platform

|  | EFFECl or | REYNOLDS | number | 2 CONDIT | ON=1 | covertid |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ANGLE | $(M E E R C \cdot M(M)$ | $\begin{aligned} & \text { RRAG } \\ & \text { (LH) } \end{aligned}$ | CD | RE/10 ${ }^{\text {5 }}$ | $\begin{aligned} & \text { AREA } \\ & (S Q . F T) \end{aligned}$ | (FET/S) |
| 0.0 | . 38 | 2.45 | 1.73 | 1.1 | 341.4 | 33.4 |
| 0.0 | . 78 | 4.11 | 1.63 | 1.5 | 341.4 | 47.8 |
| 0.0 | 1.31 | 7.85 | 1.61 | 2.0 | 341.4 | 61.9 |
| 0.0 | 1.93 | 11.51 | 1.61 | 2.4 | 341.4 | 75.1 |
| 0.0 | 3.50 | 20.14 | 1.00 | 3.2 | 341.4 | 101.0 |
| 60.0 | . 40 | 2.83 | 1.14 | 1.1 | 552.0 | 34.0 |
| 60.0 | . 71 | 4.98 | 1.16 | 1.4 | 552.0 | 45.6 |
| 60.0 | 1.31 | 4.67 | 1.11 | 2.0 | 552.0 | 61.7 |
| 60.0 | 1.80 | 11.92 | 1.11 | 2.3 | 552.0 | 72.4 |
| 60.0 | 3.56 | 23.58 | 1.11 | 3.2 | 552.1 | 101.8 |
| 60.0 | 1.32 | 8.91 | 1.13 | 2.0 | 552.0 | 61.9 |
| 60.0 | . 78 | 5.29 | 1.13 | 1.5 | 552.0 | 47.7 |
| 60.0 | . 40 | 2.70 | 1.14 | 1.1 | 55\%.0 | 34.3 |
| 160.0 | . 38 | 2.78 | 1.30 | 1.1 | 512.9 | 33.4 |
| 160.0 | . 78 | 5.41 | 1.24 | 1.5 | 512.9 | 47.8 |
| 160.0 | 1.31 | 8.90 | 1.22 | 2.0 | 512.4 | 61.9 |
| 160.0 | 1.93 | $1<.52$ | 1.17 | 2.4 | 512.9 | 75.1 |
| 160.0 | 3.50 | ? ¢.89 | 1.17 | 3.2 | 512.4 | 101.0 |
| 240.0 | . 38 | 2.00 | 1.13 | 1.1 | 552.0 | 33.4 |
| 240.0 | . 78 | 3.24 | 1.1? | 1.5 | 552.0 | 47.8 |
| 240.0 | 1.31 | 8.55 | 1.13 | 2.0 | 552.0 | 61.9 |
| 240.0 | 1.93 | 12.97 | 1.12 | 2.4 | 552.0 | 75.1 |
| 240.0 | 3.42 | 22.98 | 1.12 | 3.2 | 552.0 | 99.8 |

Table 2. Effect of Reynolds number on the drag of a four-horn cluseer (condition 1 covered platform)

| $\begin{gathered} \text { NUMBER OF } \\ \text { HORNS } \end{gathered}$ | CONDITION | PLATFORM | $\begin{gathered} \text { SEPARATION } \\ \text { FT. } \end{gathered}$ | DATA APPEARS IN |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | - | - | - | 4 | 11 |
| 1 | - | - | - | 5 | 11 |
| 1 | - | - | - | 6 | 12 |
| 2 | 3C | uncovered | 16 | 7 | 13 |
| 4 | 1 | covered | 20 | 8 | 14,15 |
| 4 | 1 | uncovered | 20 | 9 | 16 |
| 4 | 2 | uncovered | 20 | 10 | 17 |
| 4 | 3 | uncovered | 20 | 11 | 18 |
| 4 | 3A | uncovered | 16 | 12 | 20 |
| 4 | 3B | two story lower platform | 20 | 13 | 21 |

Table 3. Summary of tests
PYHAR IUAL (WITH EAHS)

$$
\begin{aligned}
& \text { QATERAL ROLL } \\
& \text { FOHCE MOMENT } \\
& \text { (I.i) }(L H \text {.FT) }
\end{aligned}
$$

350000

$$
\stackrel{\sim}{0} \underset{0}{\sim} \underset{i}{N} \underset{i}{N}
$$

$$
\underset{i}{N} \underset{\sim}{\sim} \underset{\sim}{\sim}
$$

$$
\underset{i}{\because} \overrightarrow{0}=
$$

$$
2
$$

$$
\cong 0
$$

$$
0
$$

$$
0
$$

$$
12^{\circ}
$$

Table 4. Forces and moments on a single pyramidal horn



pyramidaliwithout ears）

| angle | DYNAMIC PhFSSURE （MENC．MM） | jopag FOHCE （Li） | LATERAL FOHCE | knLL <br> MUMENT <br> （L7．FT） |  | C0） | CL | $C_{M R}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| －5．0 | 2.49 | 3.67 | －． 51 | ． 27 |  | 1.19 | －． 17 | ． 14 | 114.6 |
| 0.0 | 2.49 | 3.93 | ． 00 | ． 06 |  | 1.24 | ． 00 | ． 03 | 111.4 |
| 10.0 | 2.49 | 3.87 | ． 54 | －． 34 |  | 1.12 | ． 16 | －． 16 | 1c1．0 |
| 20.0 | 2.49 | 3.76 | ． 71 | －． 58 |  | 1.04 | ． 14 | －． 6 | 154.3 |
| 30.0 | 2.49 | 3.55 | 1.14 | －． 78 |  | ． 46 | ． 31 | －． 34 | 135.9 |
| 40.0 | 2.49 | 3.67 | .89 | －． 59 |  | 1.00 | ． 24 | －． 26 | 135.4 |
| 50.0 | 2.49 | 3.55 | ． 41 | －． 44 |  | 1.01 | － 26 | －． 20 | $1 く \%$－ |
| 60.0 | 2.49 | 3.23 | ．67 | －． 34 |  | ． 4 | ． 20 | －． 17 | 120.6 |
| 70.0 | 2.49 | 2.73 | ． 52 | －． 14 |  | ． 44 | ． 16 | －． 08 | 107．8 |
| 80.0 | 2.49 | 2.29 | .10 | ． 10 |  | ． 92 | ． 04 | .01 | 91．9 |
| 90.0 | 2.49 | 2.15 | ． 05 | ． 08 |  | 1.09 | ． 02 | ． 06 | 13.2 |
| 100.0 | 2.49 | 2.21 | －3b | －． 16 |  | ． 89 | ． 14 | －． 10 | 91．9 |
| 110.0 | 2.49 | 2.18 | ． 55 | －． 27 |  | ． 75 | ． 19 | －． 15 | 107．8 |
| 120.0 | 2.49 | 2.54 | ． 26 | －． 11 |  | ． 18 | ． 08 | －．03 | $1<0.6$ |
| 130.0 | 2.49 | 2.87 | ． 17 | －． 03 |  | － 82 | ． 05 | －．01 | 124.9 |
| 140.0 | 2.49 | 3.14 | ．1\％ | ． 01 |  | .86 | ． 05 | .00 | 135.4 |
| 150.0 | 2.49 | 3.25 | ． 24 | ． 01 |  | － 88 | .07 | －u0 | 136．9 |
| 160.0 | 2.49 | 3.28 | ． 17 | ． 01 |  | － 90 | ． 05 | ． 00 | 234.3 |
| 170.0 | 2.49 | 3.10 | －． 05 | .10 |  | ． 90 | －． 01 | －03 |  |
| 180.0 | 2.49 | 2.96 | －． 20 | ． 06 |  | ．43 | －． 06 | －us | $11 / .4$ |
| 0.0 | 2.49 | 3.183 | －． 03 | ． 08 |  | 1.21 | －． 07 | ． 04 | 11／．4 |
| 90.0 | 2.49 | 2.22 | ． 04 | ． 06 |  | 1.12 | ． 02 | ．05 | 73．2 |
|  |  | HEY | NOLDS N | NUMREK＝ | 350000 |  |  |  |  |

Table 5．Forces and moments on a single pyramidal horn （without blinders）

| Curite irre |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| angle | DYNAMIC． PRFSSURE （MEHC．MM） | DFARS <br> FOHCE （L．H） | ：ATERAL FORCE （L゙） | HOLL MUMENT （LR．FT） | co | CL | $c_{m 2}$ | $\begin{aligned} & \text { AHEA } \\ & \text { SU.F II } \end{aligned}$ |
| －5．0 | 2.49 | 3.07 | －．2？ | ． 05 | ． 84 | －． 06 | ． 02 | 135.6 |
| 0.0 | 2.49 | 3.16 | －． 13 | －．09 | ． 68 | －． 114 | －． 04 | 133.0 |
| 5.0 | 2.49 | 3.14 | ． 21 | －． 23 | ． 86 | ． 06 | －． 10 | 135．6 |
| 10.0 | 2.49 | 3.08 | ． 41 | －． 33 | ． 83 | ． 11 | －． 14 | 131．3 |
| 20.0 | 2.49 | 3.09 | ．61 | －． 43 | ． 81 | ． 16 | －．16 | 1410．6 |
| 30.0 | 2.49 | 3.01 | ． 48 | －． 35 | .19 | ． 13 | －．15 | 141．4 |
| 40.0 | 2.49 | 2.75 | ． 22 | －． 09 | .13 | ．115 | －． 04 | 140.3 |
| 50.0 | 2.49 | 2.67 | .13 | ． 03 | .73 | ． 614 | ． 01 | 13b．ts |
| 60.0 | 2.49 | 2.50 | .22 | ． 05 | ． 12 | ． 06 | ． 02 | 12せ．6 |
| 70.0 | 2.49 | 1.94 | ． 60 | －． 17 | ． 00 | ．19 | －． 09 | 114.2 |
| 80.0 | 2.49 | 1.58 | ． 24 | －． 03 | ． 54 | ． 10 | －． 01 | 101.6 |
| 90.0 | 2.49 | 1.43 | ．118 | ． 08 | － 5 | 013 | ．05 | 102．9 |
| 100.0 | 2.49 | 1.72 | －． 17 | .25 | － 59 | －．00 | ． 14 | 141.0 |
| 110.0 | 2.49 | 2.20 | －．03 | ． 16 | ． 00 | －．01 | ．08 | 11\％．2 |
| 120.0 | 2.49 | 2.44 | －3ヶ | －． 03 | ． 10 | ． 11 | －．01 | 1＜0．0 |
| 130.0 | 2.49 | 2.64 | ．${ }^{\prime}$ | －． 05 | ． 72 | －10 | －． 02 | 1s5．t |
| 140.0 | 2.49 | 2.67 | .63 | －． 00 | .11 | －11 | －． 03 | 140.3 |
| 150.0 | 2.49 | 2.58 | ． 73 | －． 13 | ． 07 | ．1\％ | －．05 | 141.0 |
| 160.0 | 2.49 | 2.47 | .64 | －． 14 | ．05 | －17 | －． 116 | 140.4 |
| 170.0 | 2.49 | 2.36 | ． 22 | －． 06 | ． 04 | ． 00 | －． 0.03 | 131.5 |
| 180.0 | 2.49 | 2.21 | －． 10 | －．01 | ． 02 | －．03 | －． 00 | 133.0 |
| 0.0 | 2.49 | 3.18 | －． 20 | －．03 | ． 84 | －．0s | －． 02 | 135.0 |
| 90.0 | 2.49 | 1.43 | ． 15 | ． 04 | ． 52 | ． 05 | ． 02 | 16ヶ．4 |
| HEYNOLDS NUMHER＝ 350000 |  |  |  |  |  |  |  |  |

Table 6．Forces and moments on a single conical horn

| CO | CL | $\mathrm{C}_{\text {jink }}$ | $\mathrm{C}_{\mathrm{MP}}$ | $\begin{gathered} \text { AHEA } \\ (\text { SQ.FT) } \end{gathered}$ | $Y_{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.65 | ． 20 | －．8y | ．92 | 110.6 | b．b |
| 1.24 | －．01 | －． 56 | － 51 | 245.6 | 4.1 |
| 1.31 | －． 10 | －． 63 | ．45 | 242.1 | 3.5 |
| 1.21 | －． 12 | －． 36 | ．$<1$ | c13．6 | c． 2 |
| 1.23 | －． 06 | －． 07 | － 20 | く15．b | 1.6 |
| $1 .<8$ | ． 02 | ．19 | ． 26 | 24 H .8 | c．1 |
| 1.24 | －．03 | ． 32 | －35 | 231.7 | ＜．0 |
| 1.24 | －． 04 | ． 5 | －bl | $28<.4$ |  |
| 1.30 | ． 04 | ． 06 | ． 64 | 254.8 | 4.1 |
| 1．32 | －． 29 | ．94 | ． 45 | 170.6 | 2.9 |
| 1.41 | －． 18 | ． 50 | ． 40 | C45．6 | ＜． 6 |
| 1．4B | ． 18 | ． 76 | ． 51 | $24<.1$ | 3.5 |
| 1.46 | ．07 | －bl | ．48 | 215.6 | 3.3 |
| 1.48 | －． 04 | ． 11 | ． 43 | ctbes | 2.4 |
| 1．50 | －． 18 | －． 38 | ． 42 | 24H．8 | 2． |
| 1.40 | ．08 | －． 38 | ． 40 | 26．1 | C．${ }^{\text {¢ }}$ |
| 1.22 | ． 26 | －． 46 | ． 41 | 28く．7 | 3.4 |
| 1．15 | ． 31 | －．53 | ． 43 | 2ち4．8 | 3. |


|  |  |  |  | COVERED |  | CONOITION＝1 |  | （20FT．SEP．） |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ANTLE | DYNAMIC PHESSIRE （NELC．NM） | $\begin{aligned} & \text { DRAG } \\ & \text { FOCCE } \end{aligned}$ (LU) | $\begin{aligned} & \text { LATERAL } \\ & \text { FUHCE: } \\ & \text { (LEO) } \end{aligned}$ | $\begin{aligned} & \text { ROLL } \\ & \text { MOMENT } \\ & (L S . F T) \end{aligned}$ | HITCH MOMENT （Lo．FT） | CD | CL | $C_{M R}$ | $C_{M P}$ | AREA （SU．FT） | $\begin{gathered} y_{D} \\ F T \end{gathered}$ |
| 0.0 | 1.67 | 9.49 | －1．21 | 1.06 | 4.12 | 1.61 | －． 19 | .27 | 1.22 | 341.4 | 7.6 |
| 20.0 | 1.67 | 9.79 | －2．15 | －H1 | 3.74 | 1.15 | －．25 | .15 | －15 | 461.1 | 6.5 |
| 40.0 | 1.67 | 11.27 | －． 46 | ． 32 | 4.30 | 1.34 | －． 12 | ． 06 | －86 | 446.0 | 6.2 |
| 55.0 | 1.67 | 11.61 | ． 01 | －． 27 | 4.11 | 1.22 | － 07 | －．05 | －6y | bえ゙ | b． 1 |
| 50.0 | 1.67 | 11.47 | 1.15 | ． 29 | 3.85 | 1.14 | －10 | －0 0 | ． 61 | bhcol | 5.4 |
| 05.0 | 1.07 | 11.17 | 1.26 | ． 77 | 3.56 | 1.14 | ． 13 | .13 | ． 28 | 511.4 | S． 1 |
| 80.0 | 1.07 | 8.106 | ． 44 | ． 34 | 2.60 | 1.13 | －0n | $.0 y$ | ． 60 | 391.3 | b． 3 |
| 100.0 | 1.57 | 7.02 | .11 | .90 | 1.84 | 1．15 | ． 02 | ． 22 | .47 | 356.1 | 3.4 |
| 120.0 | 1.07 | 4.14 | －1．44 | －．43 | 2.19 | 1.13 | －010 | －． 07 | .43 | 445.8 | 3.4 |
| 140.0 | 1.67 | 10.41 | －1．31 | ． 03 | 3.19 | 1.43 | $\cdots \cdot<1$ | .01 | －10 | 401.4 | 4.4 |
| 154．0 | 1.67 | 11.26 | －．35 | 1.14 | 3.2 c | 1.26 | －． 04 | .21 | －SH | 493.6 | 4.6 |
| 160.0 | 1.67 | 11.17 | －． 18 | 1.55 | 3.13 | 1.20 | －．02 | .21 | － 24 | $51<.9$ | 4.2 |
| 164.0 | 1.67 | 11.13 | －． 06 | 1.97 | 3.14 | 1.21 | －．01 | .34 | － 35 | bub．s | 4.5 |
| 180.0 | 1.67 | 10.11 | －．98 | 1.40 | 3.34 | 1.63 | －． 16 | － 36 | － 50 | 341.4 | 5.4 |
| 200.0 | 1.67 | 11.20 | －1．21 | －． 91 | 4.49 | 1.33 | －． 14 | ． .11 | －85． | 461.1 | 0.4 |
| 220.0 | 1.67 | 11.81 | 1.14 | －．34 | 4.98 | 1.46 | －14 | －．08 | － 48 | 446.0 | 6.7 |
| 235.0 | 1.67 | 11.83 | 2.45 | －． 51 | 4.45 | 1.24 | － 26 | －．04 | ． 15 | bib． 2 | 6.0 |
| 247.0 | 1.67 | 11.57 | 3.07 | .79 | 4.38 | 1.15 | －31 | .13 | .10 | 552．0 | 6.1 |
| 24.5 .0 | 1.67 | 11.31 | 3.54 | 1.05 | 4.06 | 1.10 | －37 | .11 | ． 61 | 331.4 | 5.6 |
| 250．0 | 1.67 | A． 60 | 1.49 | .90 | 2.41 | $1 .<1$ | － 28 | .20 | ． 54 | 341.3 | $4 \cdot 6$ |
| こッ0．0 | 1.67 | 7.95 | ． 37 | －． 17 | 1．50 | 1.23 | －00 | －． 04 | －31 | Sb6．1 | 3.0 |
| 300.0 | 1.67 | 8.49 | .77 | ． 26 | C．43 | 1.05 | ． 04 | ． 05 | ． 46 | 445.8 | 4.6 |
| 320.0 | 1.67 | 8.72 | ．82 | ． 41 | 3.17 | 1.20 | －11 | ． 09 | －6y | 401.4 | 5.6 |
| 335.0 | 1.67 | 9.42 | 1.16 | 1.24 | 3.52 | 1.05 | .13 | .22 | ． 03 | 495.6 | 6.0 |
| 345.0 | 1.67 | 9.59 | －23 | 1.71 | 4.48 | 1.04 | －02 | －30 | －18 | bob．s | 7.5 |
| 340.0 | 1.67 | 9.52 | － $\mathrm{H}_{4}$ | 1.32 | 3.08 | 1.02 | ．0y | ． 26 | .67 | 512．9 | 6.5 |
|  |  | RE | OLOS N | NUMAER＝ | 221000 |  |  |  |  |  |  |

Table 8．Experimental data for a four－horn cluster（condition 1 covered platform）

|  |  |  |  | uncoverio |  | CONOITION= |  | (COFT.SEP.) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| angle | $\begin{gathered} \text { MYNAMIC } \\ \text { PHFSSSUR } \\ \text { (MEQC.MMN) } \end{gathered}$ | $\begin{aligned} & \text { OPAG } \\ & \text { FONCE } \\ & \text { (LHE } \end{aligned}$ | $\begin{aligned} & \text { LATERN } \\ & \text { FOHCEE } \\ & \text { (LE) } \end{aligned}$ | $\begin{aligned} & \text { HOLL } \\ & \text { MOMENT } \\ & \text { (LHGFT) } \end{aligned}$ | $\begin{aligned} & \text { FITCH } \\ & \text { MOMENT } \\ & \text { (LU.FT) } \end{aligned}$ | co | CL . | $C_{M R}$ | $\mathrm{C}_{\text {im, }}$ | $\begin{gathered} \text { AREA } \\ \text { (SO.FT) } \end{gathered}$ | $\begin{aligned} & y_{D} \\ & \text { Fr. } \end{aligned}$ |
| 0.0 | 1.67 | 10.34 | -1.30 | -y | 4.40 | 1.67 | -. 21 | .23 | 1.14 | 341.4 | 6.6 |
| 20.0 | 1.67 | 9.64 | -2.01 | 1.02 | 3.22 | 1.14 | -. 24 | .19 | .61 | 461.1 | 5.3 |
| 40.0 | 1.67 | 11.64 | -. 71 | . 41 | 4.05 | 1.44 | -. 09 | . 08 | . 80 | 446.0 | 5.6 |
| 55.0 | 1.67 | 11.98 | .0H | -. 43 | 3.81 | 1.26 | . 07 | -.07 | . 04. | ¢ट¢.z | b.l |
| 60.0 | 1.67 | 12.00 | 1.11 | . 01 | 3.03 | 1.20 | . 10 | .00 | - ל | b-c. 0 | 4.8 |
| 65.0 | 1.67 | 11.40 | 1.41 | -5 | 3.22 | 1.11 | . 14 | .0y | . 33 | 531.4 | 4.5 |
| 80.0 | 1.67 | 4.56 | .44 | . 19 | 2.18 | 1.20 | .07 | . 04 | . 49 | 391.3 | 4.1 |
| 100.0 | 1.07 | 4.02 | . 010 | 1.33 | 1.74 | 1.24 | . 09 | .33 | .48 | 356.1 | 3.4 |
| 120.0 | 1.67 | 9.23 | -.41 | -. 54 | 2.ub | 1.14 | -. 11 | -. 11 | . 41 | 445.t | 3.6 |
| 140.0 | 1.67 | 10.14 | -1.c2 | -. 24 | 3.03 | 1.39 | -. 17 | -.05 | . 66 | 401.4 | 4.8 |
| 155.0 | 1.67 | 11.09 | -. 10 | 1.02 | 3.11 | 1.24 | -. 01 | .18 | . 55 | 493.6 | 4.5 |
| 100.0 | 1.67 | 11.13 | . 01 | 1.51 | 3.07 | 1.19 | . 00 | . 26 | . 53 | 512.9 | 4.4 |
| 165.0 | 1.67 | 11.15 | . 10 | 1.95 | 3.04 | 1.21 | . 01 | . 34 | . 53 | bub.s | 4.4 |
| 140.0 | 1.67 | 10.06 | -. 26 | 1.64 | 2.85 | 1.02 | -. 04 | . 42 | .13 | 341.4 | 4.5 |
| 200.0 | 1.67 | 10.98 | -1.21 | -.97 | 4.23 | 1.29 | -. 14 | -. 16 | . 80 | 461.1 | 0.2 |
| 220.0 | 1.67 | 11.35 | 1.100 | -. 21 | 4.52 | 1.40 | . 12 | -. 04 | .84 | 440.0 | 6.4 |
| 235.0 | 1.67 | 11.77 | 1.90 | . 38 | 4.40 | 1.23 | . 20 | . 06 | . 14 | b<b.c | 6.0 |
| 240.0 | 1.67 | 11.60 | 2.41 | . 54 | 4.14 | 1.16 | - ${ }^{5}$ | . 07 | .67 | 532.0 | 5.8 |
| 245.0 | 1.67 | 11.31 | 2.72 | . 74 | 3.87 | 1.16 | . 28 | -1く | .63 | 537.4 | b.b |
| 260.0 | 1.67 | 8. $\mathrm{H}^{2}$ | 1.17 | .53 | 2.17 | 1.24 | . 10 | . 12 | -4y | -341.3 | 3.4 |
| 280.0 | 1.07 | 7.50 | . 14 | . 24 | 1.10 | 1.10 | . 02 | . 06 | - $\mathrm{CH}^{\text {c }}$ | 366.1 | 2.5 |
| 300.0 | 1.67 | 8.93 | . 11 | . 34 | 1.45 | 1.10 | . 01 | . 01 | -34 | 445.8 | 3.5 |
| 320.0 | 1.67 | 9.32 | . 26 | . 29 | 2.58 | 1.28 | . $0+$ | . 00 | -bl | 401.4 | 4.4 |
| 335.0 | 1.67 | 10.55 | . 13 | 1.14 | 3.14 | 1.18 | . 01 | . 20 | . 60 | 493.6 | b.l |
| 340.0 | 1.67 | 10.76 | -.02 | 1.44 | 3.00 | 1.16 | -. 00 | - 26 | . 63 | blc.s | b.4 |
| 345.0 | 1.67 | 10.80 | -. 21 | 1.61 | 4.04 | 1.18 | -.02 | -28 | .11 | sub.s | 6.1 |
| HEYNOLOS NUMHER $=221000$ |  |  |  |  |  |  |  |  |  |  |  |

Table 9. Experimental data for a four-horn cluster (condition 1 uncovered platform)
CONDITION=2 (20FT.SEP.)




| CONUITION=3 |  | (COFT.SEP. |  | area |
| :---: | :---: | :---: | :---: | :---: |
| CD | CL | $\mathrm{C}_{\text {M }}$ | $c_{\text {inp }}$ |  |
|  |  |  |  | (SU.FT) |
| 1.71 | . 20 | -. 37 | 1.21 | 304.9 |
| 1.17 | . 02 | -. 17 | -6 | 464.7 |
| 1.12 | -. 02 | -. 11 | - | 416.0 |
| $1 .<4$ | -. $0<$ | -. 12 | -6b | $19<.8$ |
| 1.01 | . 01 | -. 09 | .4H | 314.5 |
| 1.14 | -.03 | -.03 | . 42 | $4 \mathrm{Cb.4}$ |
| 1.27 | -.10 | .01 | -t8 | 318.3 |
| 1.07 | -. 15 | -. 15 | - 50 | 518.5 |
| 1.01 | -. 17 | .03 | . 19 | 451.5 |
| 1.13 | -. 04 | . 30 | . 62 | 305.4 |
| 1.31 | -. 16 | . 30 | .77 | 304.9 |
| 1.28 | -.22 | -. 16 | . 46 | 404.7 |
| 1.c1 | -. 10 | -. 10 | .48 | 416.0 |
| 1.50 | -. 10 | . 19 | -12 | 392.8 |
| 1.24 | - | . 29 | . 54 | 314.5 |
| 1.43 | .0y | . 31 | . 01 | 4 cb.9 |
| 1.40 | . 10 | .0y | . 04 | 378.3 |
| 1.313 | . 00 | b0 0 | -11 | 518.5 |
| 1.47 | . 34 | . 04 | . 62 | ל451.5 |
| 1.08 | . 37 | .00 | -by | bus.4 |

مُ




[^1]оэязлоэлn



|  |  |  |  | uncovered |  | CONOITION=3B 12 |  |  | OFT.StP.) Two |  | story |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ANGLE | $\begin{aligned} & \text { OYNAMIC } \\ & \text { PYFSSSUQE } \\ & \text { (NERC.MMM) } \end{aligned}$ | DRAG FONCE (LB) | LATERAL FOHCE (LH) | $\begin{aligned} & \text { KOLL } \\ & \text { MOMENT } \\ & \text { URGOF } \end{aligned}$ (LHOFT) | $\begin{aligned} & \text { PITCH } \\ & \text { MOMENT } \\ & \text { (LH.FT) } \end{aligned}$ | co | CL | $\mathrm{C}_{\mu \mathrm{NR}}$ | $\mathrm{C}_{\text {m }} \mathrm{P}$ | $\begin{gathered} \text { AREA } \\ \text { (SQ.FT) } \end{gathered}$ | $\begin{aligned} & Y_{D} \\ & f_{t} \end{aligned}$ |
| 0.0 | 1.70 | 4.61 | 1.33 | -.n5 | 3.91 | 1.72 | . 24 | -. 19 | 1.12 | 304.9 | 0.5 |
| 20.0 | 1.70 | 9.29 | . 71 | -. 47 | $3.11^{\circ}$ | 1.09 | .08 | -. 09 | - | 404.7 | b.4 |
| 40.0 | 1.70 | 9.10 | . 49 | -. 92 | 2.10 | 1.26 | . 07 | -. 20 | . 60 | 392.8 | 4.1 |
| 60.0 | 1.70 | 9.94 | . 17 | -. 06 | 2.15 | 1.05 | . 02 | -. 01 | - 30 | 314.5 | 3.5 |
| 50.0 | 1.70 | 9.00 | -. 33 | -. 29 | 1.47 | 1.15 | -. 04 | -. 06 | . 30 | $4<3.9$ | 2.6 |
| 100.0 | 1.70 | H.66 | -.0n | . 26 | 2.06 | 1.25 | -. 12 | . 06 | . 47 | 118.3 | 3.4 |
| 120.0 | 1.70 | 9.49 | -1.84 | -. 71 | 2.74 | 1.00 | -. 19 | -. 12 | . 47 | 518.5 | 4.1 |
| 140.0 | 1.70 | 9.87 | -1.15 | . 13 | 3.35 | 1.15 | -. 14 | . 03 | -6b | 451.5 | 3.4 |
| 150.0 | 1.70 | 9.92 | -. 67 | 1.09 | 3.31 | 1.07 | -. 07 | . 19 | . 51 | 505.4 | 5.3 |
| 180.0 | 1.70 | \%.79 | -1.00 | .5y | 2.86 | 1.51 | . .18 | .11 | - ${ }^{\text {b }}$ | 304.9 | 5.2 |
| 200.0 | 1.70 | 10.55 | -1.42 | -.83 | 2.71 | 1.24 | -. 17 | -. 16 | -bl | 464.7 | 4.1 |
| 220.0 | 1.70 | 9.80 | . 35 | . 54 | 3.28 | 1.36 | . 05 | . 12 | .13 | 342.8 | 5.3 |
| 240.0 | 1.70 | 9.44 | . 34 | -. 34 | 3.42 | 1.30 | .03 | -.00 | . 90 | 318.3 | 0.6 |
| 300.0 | 1.70 | 10.19 | -1.00 | . 08 | 4 ל-b | 1.01 | -. 11 | . 01 | . 10 | 518.5 | 1.1 |
| 320.0 | 1.70 | 10.87 | 2.30 | -. 16 | 4.b7 | 1.31 | . 28 | -.03 | . 88 | 451.5 | 0.1 |
| 340.0 | 1.70 | 4.07 | 3.27 | -. 53 | 3.98 | . 48 | . 36 | -. 09 | . 64 | 305.4 | 7.0 |
|  |  | HEy | NOLOS N | NUMPER= | 240000 |  |  |  |  |  |  |

Table 13. Experimental data for a four-horn cluster with an upper platform (two story cluster, Condition 3B)

## APPENDIX

DESCRIPTION OF THE HORNS, ANTENNA AND CONFIGURATIONS SUPPLIED BY THE SPONSOR


Fig. Al Dimensions of the pyramidal horn

PROJECTED AREAS IN SQ. FT. ( $20^{\prime}-0^{\prime \prime}$ SEPARATION)
6 Corporate Park Drive, White Plains, New York 10604
Project: $\qquad$
$\square$


6 Corporate Park Drive, White Plains, New York 10604
Sheet No. $\qquad$
Date 8/11/76
By $\qquad$
Project: PROJECTED AREA OF AFC, CH-10 CONICAL ANTENMA INCLUDING MDUNTING RING


Fig. A2 Dimensions of the conical horn

Rose, Chulkoff \& Rose
Structural Engineers

Sheet No 1 Of 3
Date $\mathbf{7 / 3 0 / 7 6}$
By $\qquad$
6 Corporate Park Drive, White Plains, New York 10604

Project: $\quad$ PROJECTED AREAS in SQ. FT. ( 161 - 0 " SEPARATION)


## CONDITION 1

PROJECTED AREAS OF HORNS, MOUNTING FRAMES \& PLATFORM


CONDITION 2
PROJECTED AREAS OF HORNS, MOUNTING FRAMES \& PLATFORM


CONDITION 3
PROJECTED AREAS OF HORNS, MOUNTING FRAMES \& PLATFORM


PROJECTED AREAS OF EORAS, MDUIIIMG FRAMES \& PLATFORM


CONDITION $3 C$
( $16^{\prime}-0^{-1}$ Separation)
PROJECTED AREAS OF HORNS, MOUNTING FRAMES \& PLATFORM



Fig. 31. Drag coefficient of sheet-metal "caps" (40,a) as a function of their height ratio.

Caps and Cups. As large as the drag coefficients of plates may be, there are other shapes exhibiting still higher values. Figure 31 shows the drag coefficient of open cup- or cap-like bodies (similar to parachute canopies). The maximum drag coefficient (on projected area) is obtained for $h / d$ in the order of 0.5 , a shape which is $\approx$ hemispherical. Upon further increasing the height ratio, the rear side more and more changes into a wake "fairing". The drag coefficient is, therefore, expected to approach the theoretical minimum which corresponds to full stagnation pressure across the opening.

## 7. DRAG OF WEDGES AND CONES

Figures 32 and 33 present shape and drag coefficient of a number of three- and two-dimensional bodies. All of these shapes have a more or less separated flow pattern; most of them have negative pressure on their rear side; and their drag coeflicients are comparatively high.

Angle of Flow. To establish some order in the drag coeflicients of various shapes, the geometrical angle is very useful, at which the flow is guided by the body's surface upon separating from its rear side. The flat plate, for example, has such an angle " $\varepsilon$ " $=90^{\circ}$. A "fold" with a vertex angle of two times $45^{\circ}$, has a separation angle of $90^{\circ}$ plus or minus $45^{\circ}$, depending upon the direction of the oncoming flow. Figure 34 demonstrates how the drag coefficient increases as a function of the shape angle. Two branches are found, of course; one for two-dimensional bolies (between walls) and another one for three-dimensional conditions. $\mathrm{At}^{*}{ }^{\circ} \varepsilon^{*}=0$, parallelsided round-nosed shapes have been used in the graph; a hallow, scoop-like body is plotted at $180^{\circ}$.

Figure 32 (near). Drag coefficients of various 3dimensional bodies (40) at R'numbers between $10^{4}$ and $10^{6}$. Note: (o) tested on wind-tumel floor.

IT (37) Information on rear-side pressure of plates:
a) On disks and small-aspect-ratio plates see: NACA (36,
a); AVA Ergebnisse IV; reference ( $40, \mathrm{I}$ ).
b) On plates between walls see: (12), ( $35, a)$ and ( 40,1 ). IT (40) Experimental results on three-dimensional bodies:
a) Doetsch, Parachute Models, Lufo 1938 p. 577.
b) NACA, Cup Anemometer, Tech Rpt 513 (1935).
c) AVA, Hemispherical Bodies, Ergebnisse IV (1932).
d) Eiffel, Recherches a Tour Eiffel, Paris 1907.
e) Hemispherical Cup at $\mathrm{K}_{\mathrm{d}}=210^{5}$, ARC RM 712 (1919).

1) Imminger and Nokkentved, Elementary Bodies and Buildings, Kopenhagen 1930 and 1936; Transl'n by Jarvis. $\pi(11)$ Sections (tested between plates or walls):
a) Lindsey, Simple Shapes, NACA T. Rpt 619 (1940).
b) Junkers Wind-Tunnel, Report Ströte V. 9609 (1940).
c) Interierence Between Struts, NACA T. Rpt 468 (1933).
d) Delany-Sorensen, Various Shapes, NACA T.Note 3038.
e) AVA Göttingen, Ergebnisse II (1923) and III (1926).
2) Junkers Wind-Tunnel Result on Angle Profile.
g) Reported by Barth, Zt.Flugwissen 1954 p. 309.

If (42) Free-streamline (cavitation) theory:
a) Kirchhoff, Free Jet Theory, Crelle 1869 (see Lamb).
b) Bobyleff, Russian Phys. Chem. Society 1881 (see Lamb). c) Riabouchinsky-Plesset-Schafer, Journal Appl.Physics 1948 p.934, and Review Modern Physics 1948 p. 228 .
d) Reichardt, Laws of Cavities, German ZWB UM 6628. II (43) Neel, Dive Brakes, Fieseler Tunnel Rpt 22 (1941).

Figure 33 (right). Drag coefficients (41) of 2 dimensional shapes (between walls) at $R$ between $10^{4}$ and $10^{6}$. Note: (+) in subcritical flow.



[^0]:    *Laboratory Simulation of the Atmospheric Boundary Layer. AIAA Journal, Vol. 9, No. 9, Sept. 1971. pp 1746-1754.

[^1]:    000922

