## ColoradoState University

Finance \& Real Estate

## Financial Risk Management

MSBA in Financial Risk Management


## Further Discussion On Simulation



## ColoradoStateUniversity

## Numerical Integration



## Shared Birthdays

- There are 30 people in a room ... what is the chance that any two of them celebrate their birthday on the same day? Assume 365 days in a year.




## The Minimum Iterations to Run

- A short answer, burdened with many caveats, is "no less than 300'. At 300 iterations you start to get a reasonably well defined cumulative distribution

300 iterations


3000 iterations


## How Many Iterations to Run

In general, you'll have two opposing pressures:

- Too few iterations and you get inaccurate outputs, graphs (particularly histogram plots) that look "scruffy';
- Too many iterations and it takes a long time to simulate, and it may take even longer to plot graphs, export and analyze data, etc. afterwards.

$$
\mu=N(\bar{x}, \sigma / \sqrt{n})
$$

$$
n>\left(\frac{\sigma^{*} z}{\delta}\right)^{2}
$$

## ColoradoStateUniversity

## Precision Control



X

## Define Forecast: Cell D9

Run Preferences

1000

95 $\square$ $\%$

Number of trials to run
$\checkmark$ Stop on calculation errors
$\checkmark$ Stop when precision control limits are reached

## Trials Samplina Speed Options Statistics <br> Trials Samplina Speed Ontions Statistics

## Confidence level



## The Chi-Squared Goodness-of-Fit Statistic

- The Chi-squared statistic measures how well the expected frequency of the fitted distribution compares with the observed frequency of a histogram of the observed data.

$$
x^{2}=\sum_{i} \frac{(O(i)-E(i))^{2}}{E(i)}
$$



## Kolmogorov-Smirnoff (K-S) Statistic

The K-S statistic $D n$ is defined as:

$$
D n=\max [|F n(x)-F(x)|]
$$

## where

$D n$ is know as the $\mathrm{K}-\mathrm{S}$ distance

$n=$ total number of data points
$F(x)=$ distribution function of the fitted distribution
$F n(x)=i / n$
$i=$ the cumulative rank of the data point

## Anderson-Darling (A-D) Statistic

The A-D statistic is defined as:

$$
A_{n}^{2}=\int_{-\infty}^{\infty}\left|F_{n}(x)-F(x)\right|^{2} \Psi(x) \cdot f(x) \cdot d x
$$

where $\quad \Psi(x)=\frac{n}{F(x) \cdot\{1-F(x)\}}$
$n=$ total number of data points
$F(x)=$ distribution function of the fitted distribution
$f(x)=$ density function of the fitted distribution
$F n(x)=i / n$
$i=$ the cumulative rank of the data point

## Colorado StateUniversity

## Define Correlations



## Crystal Ball Tools

## Batch Fit

The Batch Fit tool lets you "automatically" fit (continuous) probability distributions to multiple data series.

## Correlation Matrix

The Correlation Matrix lets you enter a matrix of correlations between assumptions in one step.

## Tornado Chart

The Tornado Chart Tool allows you to determine the impact of each model variable (one at a time) on one specific forecast.

## Bootstrap

Crystal Ball's Bootstrap tool looks at how robust your simulation forecast statistics are. For example, given that you have done 10,000 iterations, the Bootstrap Tool determines how precisely the forecast statistics have been determined, meaning by how much would those statistics change if one were to run an essentially infinite number of iterations.

## Crystal Ball Tools

## Decision Table

The Decision Table tool allows you to run multiple simulations to test different values of one or two decision variables.
Scenario Analysis
The Scenario Analysis Tool allows you to examine which combination of assumption values gives you a certain forecast result. The tool runs a simulation after which it matches all the forecasts with their corresponding assumption values. In the resulting table, it shows all the forecast values in the range you specified (e.g. between $95 \%$ and $100 \%$ percentile) sorted, along with all the corresponding assumption (input) values. This tool can therefore be used as one of the methods to get a better understanding of an output of a simulation.

## Two dimensional Simulation

The Two-Dimensional Simulation Tool in Crystal Ball lets you separate the effect of uncertainty (lack of knowledge) and variability and randomness in a forecast.

## Predictor



Tianyang Wang

## Measures of Accuracy

- The forecast error is the difference between the actual value and the forecast, $E_{\mathrm{t}-k, t}=Y_{\mathrm{t}}-F_{t-k, t}$.
- Forecasting software packages report several summary measures of the forecast errors.
- Mean Absolute Error:

$$
\mathrm{MAE}=\left(\sum_{t=1}^{N}\left|E_{t}\right|\right) / N
$$

- Root Mean Square Error: $\mathrm{RMSE}=\sqrt{\left(\sum_{t=1}^{N} E_{t}^{2}\right) / N}$
- Mean Absolute Percentage Error:

$$
\text { MAPE }=100 \% \times\left(\sum_{t=1}^{N}\left|E_{t} / Y_{t}\right|\right) / N
$$

- One other measure of the forecast error is the average of all errors.


## Determining Performance

- Theil's $\boldsymbol{U}$ determins the forecasting performance of the model.
- The interpretation in daily language is as follows:
- Interpret (1- Thei'I U)
- $1.00-0.80$ High (strong) forecasting power
- $0.80-0.60$ Moderately high forecasting power
- $0.60-0.40$ Moderate forecasting power
- 0.40-0.20 Weak forecasting power
- $0.20-0.00$ Very weak forecasting power


## Boot Strap



## Jackknife

- The Bootstrap was originally developed from a much earlier technique called the Jackknife, invented by the brilliant and practical statistician John Wilder Tukey (1915-2000). The Jackknife was used to review the robustness of a statistic calculated from a set of data.
- A Jackknife value was the statistic of interest calculated with the ith value removed from the data set and is given the notation $\theta(\mathrm{i})$. With a data set of n values, one thus has n Jackknife values, the distribution of which gives a feel for the uncertainty one has about the true value of the statistic. We say "gives a feel" because the reader is certainly not recommended to use the Jackknife as a method for obtaining any precise estimate of uncertainty. The Jackknife turns out to be an awful estimation of uncertainty.
- like a physical jack-knife (a compact folding knife), it is a rough-and-ready tool that can improvise a solution for a variety of problems even though specific problems may be more efficiently solved with a purpose-designed tool.


## The "analytics" realm



What happened


## Probability distributions in simulation modeling

Heterogeneity/inter-individual variability: collection of differences between individuals/entities e.g. Heights, Income, FICO scores

Randomness/variability: differences observed due to chance.
Natural: inherent to the system evaluated e.g. equipment failure rates, loan defaults, natural disasters
Artificial: sampling. e.g. quality control, surveys


Uncertainty: What we don't know. Unlike two above, a function of the observer.
Thus, can be reduced as more data is collected e.g. Demand growth, stock drift, true prevalence of a disease



## ORACLE <br> CRYSTAL BALL

## Applications with Crystal Ball

## Walton Bookstore Using Crystal Ball

- Let's assume a different demand distribution this time.
- Demand follows a triangular distribution with

| Demand distribution - triangular |  |
| :--- | ---: |
| Minimum | 100 |
| Most likely | 175 |
| Maximum | 300 |

## ColoradoStateUniversity

## Crystal Ball Examples



## Crystal Ball Examples Guide

| Model Name | Industry | Application | Product Demonstrated | Feature <br> Demonstrated |
| :---: | :---: | :---: | :---: | :---: |
| Cell Phone |  |  | Crystal Ball simulation Crystal Ball Tools | Sensitivity Analysis |
| Cost Estimation | Construction | Project Management Cost Estimation | Developer Kit |  |
| Critical Path | Consumer Goods | Project Management Six Sigma | Crystal Ball simulation <br> Developer Kit | Cell Referencing Crystal Ball Functions |
| DCF Analysis | Pharmaceuticals | Financial Analysis <br> Valuation | Crystal Ball simulation | Trend Chart |
| DFSS Fluid Pump | Manufacturing | Design For Six Sigma (DFSS) | OptQuest | Capability Metrics Scatter Charts |
| Drill Bit Replacement | Mining Oil \& Gas |  | OptQuest |  |
| Futura Apartments | - |  | Crystal Ball simulation Crvstal Ball Tools | Bootstrab |

## Vision Research

- Vision Research has completed preliminary development of a new drug, code-named ClearView, that corrects nearsightedness. This revolutionary new product could be completely developed and tested in time for release next year if the FDA approves the product.
- Uncertainty around costs, \# of patients cured, and market potential for product
- Should the company scrap the ClearView project or proceed to develop and market this revolutionary new drug?


## Vision Research

## Pharmaceutical Research - ClearView Project

|  |  | Suggested Assumptions: |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Costs (in millions) |  |  |  |  |  |
| Development Cost of ClearView to Date | \$10.0 |  | P1 ${ }^{\text {² }}$ | P2 | P3 |
| Testing Costs | \$4.0 | Uniform | \$3 | \$5 |  |
| Marketing Costs | \$16.0 | Triangular | \$12 | \$16 | \$18 |
| Total Costs | \$30.0 |  |  |  |  |
| Drug Test (sample of 100 patients) |  |  |  |  |  |
| Patients Cured | 100 | Binomial | 25\% | 100 |  |
| FDA Approved if 20 or More Patients Cured | TRUE |  |  |  |  |
| Market Study (in millions) |  |  |  |  |  |
| Persons in U.S. with Nearsightedness Today | 40.0 |  |  |  |  |
| Growth Rate of Nearsightedness | 2.00\% | Custom | 0\% | 5\% | 75\% |
| Persons with Nearsightedness After One Year | 40.8 |  | -15\% | -5\% | 25\% |
| Gross Profit on Dosages Sold |  |  |  |  |  |
| Market Penetration | 8.00\% | Normal | 8\% | 2.0\% |  |
| Profit Per Customer in Dollars | \$12.00 |  |  |  |  |
| Gross Profit if Approved (MM) | \$39.2 |  |  |  |  |
| Net Profit (MM) | \$9.2 |  |  |  |  |

$$
\text { ェanyang Wang FIN } 670
$$

## DCF Analysis

- Your pharmaceutical company is very interested in acquiring AllergyGone, a potential new anti-allergy drug with no known side effects. You have been asked to produce a Discounted Cash Flow (DCF) analysis of AllergyGone over a five-year period to determine if this product is worth acquiring.
- Because of the uncertainty in the product pricing, demands, and costs, your company has decided to use Crystal Ball to simulate the Net Present Value (NPV) and Internal Rate of Return (IRR) prior to negotiations. Crystal Ball can help you determine a bottom-line negotiation price and the model variables that drive the variability in the NPV and IRR forecasts.


## Inventory Management

- In inventory systems, demand is usually uncertain, and the lead time can also vary. To avoid shortages, managers often maintain a safety stock. In such situations, it is not clear what order quantities and reorder points will minimize expected total inventory cost.
- Uncertainty around weekly product demand
- Use Crystal Ball to determine the range of expected costs and quantify the impact of changes in order policy.



## Brain Teaser...

- A) The average number of tosses until HTH is larger than the average number of tosses until HTT.
- B) The average number of tosses until HTH is the same as the average number of tosses until HTT.
- C) The average number of tosses until HTH is smaller than the average number of tosses until HTT.


## ColoradoStateUniversity

## House Sales



## Soft Drink Sales



# ColoradoState University <br> <br> Magazine Sales 

 <br> <br> Magazine Sales}

## Magazine Checkout Sales

|  | Magazine $\boldsymbol{A}$ | Magazine $\boldsymbol{B}$ | Magazine $\boldsymbol{C}$ | Magazine $\boldsymbol{D}$ |
| :--- | ---: | ---: | ---: | ---: |
| Sales Volume | 562 | 362 | 646 | 508 |
| Retail Price | $\$ 4.95$ | $\$ 7.95$ | $\$ 3.95$ | $\$ 5.95$ |
| Cost of Goods | $\$ 2.20$ | $\$ 3.80$ | $\$ 1.95$ | $\$ 2.40$ |
| Gross Profit | $\$ 1,546$ | $\$ 1,502$ | $\$ 1,292$ | $\$ 1,805$ |

Total Gross Profit: $\$ 6,144$

## ColoradoStateUniversity

## Cartoon



