THESIS

DAM OVERTOPPING AND FLOOD ROUTING
WITH THE TREX WATERSHED MODEL

Submitted by
Andrew Steininger
Department of Civil and Environmental Engineering

In partial fulfillment of the requirements
For the Degree of Master of Science
Colorado State University
Fort Collins, Colorado
Spring 2014

Master’s Committee:
Advisor: Pierre Y. Julien
Jeffrey Niemann
Stephanie Kampf
ABSTRACT

DAM OVERTOPPING AND FLOOD ROUTING
WITH THE TREX WATERSHED MODEL

Modeling dam overtopping and flood routing downstream of reservoirs can provide basic information about the magnitudes of flood events that can be beneficial in dam engineering, emergency action planning, and floodplain management. In recent years there has been considerable progress in computer model code development, computing speed and capability, and available elevation, vegetation, soil type, and land use data which has led to much interest in multi-dimensional modeling of dam failure, overtopping, and flood routing at the watershed scale.

The purpose of this study is to ascertain the capability of the Two-dimensional, Runoff, Erosion and Export (TREX) model to simulate flooding from dam overtopping as the result of large scale precipitation events. The model has previously been calibrated for the California Gulch watershed near Leadville Colorado and was used for all of the simulations preformed for this study. TREX can simulate the reservoir filling and overtopping process by inserting an artificial dam into the digital elevation model (DEM) of a watershed.

To test the numerical stability of the model for large precipitation events, point source hydrographs were input to the model and the Courant-Friedrichs-Lewy (CFL) condition was used to determine the maximum numerically stable time steps. Point sources as large as 50,000 m³/s were stably routed utilizing a model time step as small as
0.004 seconds. Additionally the effects of large flows on the flood plain were analyzed using point source hydrographs. The areal extent of floodplain inundation was mapped and the total areal extent of flooding was quantified.

The attenuation of watershed outlet discharge due to upstream dams was analyzed. Three probable maximum precipitation (PMP) events and three estimated global maximum precipitation (GMP) events (the 1 hour, 6 hour, and 24 hour duration events), were simulated. Larger duration rainstorms had lower rainfall intensities but larger runoff volumes. A series of artificial dams ranging from 5 to 29 meters high were inserted into the DEM in sequential simulations and the attenuation of the downstream flood wave was quantified. The maximum attenuation of the peak discharge at the outlet of the watershed was 63% for an 18 meter high rectangular dam for the 1 hour PMP event, 58% for a 20 meter high dam for the 6 hour PMP event, and 46% for a 29 meter high dam for the 24 hour duration PMP event. The same analysis was done using estimated global maximum precipitation (GMP) events. The maximum attenuation of the peak discharge at the outlet of the watershed was 59% for a 23 meter high rectangular dam for the 1 hour GMP event, 21% for a 29 meter high dam for the 6 hour GMP event, and 9% for a 29 meter high dam for the 24 hour duration GMP event.
ACKNOWLEDGMENTS

I would like to thank everyone who helped me both directly and indirectly with my thesis work that is presented here. The support that I’ve received in both a scholarly sense and in my personal life has greatly helped me in my pursuit of a civil engineering degree from Colorado State University.

Thanks firstly to my advisor Dr. Pierre Julien who allocated the necessary funding for my research and provided me with direction and advice to accomplish this research work. Thanks also to my peers within the civil engineering department and specifically within Dr. Julien’s group. Thanks to Jazuri Abdullah and Jaehoon Kim for their routine help with my research. Thanks also to Mark Velluex for the help I received while learning to operate the model used for my research.

Thanks also to the Department of Defense Center for Geosciences and Atmospheric Research (CGAR) for the funding that was provided for this research and for the opportunities granted within this research group.

Finally thanks to those of my friends and family who helped me along the way with words of wisdom and motivation. This support provided much needed perspective and inspiration along the way.
# TABLE OF CONTENTS

ABSTRACT ........................................................................................................................................ II

ACKNOWLEDGMENTS ....................................................................................................................... IV

TABLE OF CONTENTS ....................................................................................................................... V

LIST OF TABLES ................................................................................................................................ VIII

LIST OF FIGURES ............................................................................................................................... IX

CHAPTER I. INTRODUCTION ........................................................................................................ 1

   SECTION 1.1 Overview .................................................................................................................. 1

   1.1.1 Dam Breach and Overtopping (The Problem) ................................................................. 2

   1.1.2 Modeling Dam Overtopping and Flood Routing .............................................................. 4

   SECTION 1.2 Objectives ............................................................................................................... 4

CHAPTER II. LITERATURE REVIEW ............................................................................................ 5

   SECTION 2.1 Dam Breach Modeling Techniques Overview .................................................... 5

   2.1.1 Dam Breach Empirical Models ......................................................................................... 5

   2.1.2 Dam Break Analytical Models .......................................................................................... 9

   2.1.3 Dam Breach Computer Models ....................................................................................... 11

   2.1.4 Watershed Computer Models ........................................................................................ 13

CHAPTER III. The Two-Dimensional Runoff Erosion and Export Model ....................... 17

   SECTION 3.1 TREX Conceptual Model .................................................................................... 17

   SECTION 3.2 Hydrologic Process Descriptions ........................................................................ 18

   3.2.1 Precipitation and Interception ....................................................................................... 18
LIST OF TABLES

Table 1.1:  Selected dam failures (Association of Dam Safety Officials) .......................................................... 2

Table 2.1:  Summary of dam breach hydrograph empirical relationships (Thornton et al. 2011) ................................................... 7

Table 2.2:  Physically-based embankment breach parameters (Wahl 1998) .................................................. 11

Table 5.1:  Multi-watershed time step stability data ................................................................................................................. 46

Table 6.1:  Summary of PMP simulation results .......................................................................................................................... 70

Table 6.2:  Summary of GMP simulation results .......................................................................................................................... 76
LIST OF FIGURES

Figure 1.1: Relative number of dam failures due to a variety of mechanisms ..................... 3
Figure 2.1: Dam failure data sets (Thornton et al. 2011) .................................................. 7
Figure 2.2: Predicted time of failure vs. observed time of failure ........................................ 9
Figure 3.1: TREX conceptual model structure and simulated processes .............................. 18
Figure 4.1: Study site location, California Gulch, Colorado (Velleux 2005) ......................... 27
Figure 4.2: California Gulch watershed and Leadville Colorado ........................................... 28
Figure 4.3: California Gulch digital elevation model ............................................................ 30
Figure 4.4: California Gulch aspect map ............................................................................. 31
Figure 4.5: California Gulch slope map ................................................................................ 31
Figure 4.6: California Gulch link map .................................................................................. 32
Figure 4.7: California Gulch land use type map .................................................................... 33
Figure 4.8: California Gulch soil type map .......................................................................... 34
Figure 4.9: California Gulch gaging stations ....................................................................... 35
Figure 4.10: California Gulch hydrologic calibration ............................................................ 36
Figure 4.11: California Gulch hydrologic validation ............................................................. 37
Figure 5.1: Typical approximated point source hydrograph .................................................. 38
Figure 5.2: Numerical model domains (Schär 2014) ............................................................. 40
Figure 5.3: TREX, California Gulch point source stability .................................................... 41
Figure 5.4: Model stability watershed comparison (Kim 2012) (Abdullah 2013) .................. 45
Figure 5.5: 5 meter high dam breach simulation .................................................................. 50
Figure 5.6: 4,000 m$^3$/s point source .................................................................................. 52
Figure 5.7: 4,000 m$^3$/s point source (zoom 1) ................................................................. 53
Figure 5.8: 4,000 m$^3$/s point source (zoom 2) ................................................................. 54
Figure 5.9: 4,000 m$^3$/s point source floodplain inundation at selected time steps, (depth ≥ 1 meter) ......................................................................................................................... 55
Figure 5.10: 7,000 m$^3$/s point source floodplain inundation ............................................. 56
Figure 6.1: Rectangular and Triangular profile dam examples as seen from above .......... 61
Figure 6.2: California Gulch artificial dam site location .................................................. 62
Figure 6.3: Three-dimensional dam representation ......................................................... 62
Figure 6.4: Overtopping simulation ................................................................................. 64
Figure 6.5: Example model output .................................................................................. 65
Figure 6.6: 1 hour duration PMP outlet discharge ......................................................... 67
Figure 6.7: 1 hour duration PMP peak outlet discharge vs. dam height ......................... 67
Figure 6.8: 6 hour duration PMP outlet discharge ......................................................... 68
Figure 6.9: 6 hour duration PMP peak outlet discharge vs. dam height ......................... 68
Figure 6.10: 24 hour duration PMP outlet discharge ..................................................... 69
Figure 6.11: 24 hour duration PMP peak outlet discharge vs. dam height ..................... 69
Figure 6.12: World’s greatest measured precipitation .................................................... 71
Figure 6.13: 1 hour duration GMP outlet discharge ....................................................... 73
Figure 6.14: 1 hour duration GMP peak outlet discharge vs. dam height ...................... 73
Figure 6.15: 6 hour duration GMP outlet discharge ....................................................... 74
Figure 6.16: 6 hour duration GMP peak outlet discharge vs. dam height ...................... 74
Figure 6.17: 24 hour duration GMP outlet discharge ..................................................... 75
Figure 6.18: 24 hour duration GMP peak outlet discharge vs. dam height ..................... 75
LIST OF SYMBOLS

\( A_c \) = cross sectional area of flow

\( A_s \) = surface area over which the precipitation occurs

\( B_x, B_y \) = flow width in the x- or y- direction

\( c \) = celerity

\( C \) = Courant number

\( D_c \) = dam crest height

\( dt \) = time step for numerical integration

\( dx \) = modeled raster cell size

\( E \) = evaporation rate

\( f \) = infiltration rate

\( F \) = cumulative (total) infiltrated water depth

\( g \) = gravitational acceleration

\( h \) = surface water depth

\( h_d \) = drop in reservoir surface level

\( H_c \) = capillary pressure (suction) head at the wetting front

\( H_d \) = Height of a dam

\( H_w \) = hydrostatic pressure head (depth of water in channel)

\( H_b \) = Height of the water behind the dam

\( i \) = precipitation rate

\( i_n \) = net effective precipitation rate

\( k_b \) = mean erosion rate of a dam breach
\( K_h \) = effective hydraulic conductivity
\( L \) = embankment length
\( n \) = Manning roughness coefficient
\( P_c \) = wetted perimeter of channel flow
\( q_l \) = lateral unit discharge (into or out of the channel)
\( q_x, q_y \) = unit discharge in the x- or y- direction = \( Q_x/B_x \), \( Q_y/B_y \)
\( Q_x, Q_y \) = flow in the x- or y- direction
\( Q \) = total discharge
\( Q_p \) = peak discharge
\( R_h \) = hydraulic radius of flow = \( A_c/P_c \)
\( S_{fx}, S_{fy} \) = friction slope in the x- or y- direction
\( S_{0x}, S_{0y} \) = ground surface slope in the x- or y- direction
\( s |_{t+dt} \) = value of the model state variable at time \( t + dt \)
\( s |_t \) = value of the model state variable at time \( t \)
\( S_i \) = interception capacity of projected canopy per unit area
\( S_e \) = effective soil saturation
\( t \) = time
\( t_f \) = time of dam failure
\( t_l \) = transmission loss rate
\( t_p \) = time to peak discharge
\( t_r \) = precipitation duration
\( T \) = cumulative (total) depth of water transported by transmission loss
\( u \) = flow velocity
\( V_s \) = volume of water stored behind the dam at capacity

\( V_i \) = interception volume

\( V_g \) = gross precipitation water volume

\( V_n \) = net precipitation

\( W \) = unit discharge from/to a point source/sink

\( W_{ave} \) = average embankment width

\( \alpha_x, \alpha_y \) = resistance coefficient for flow in the x- or y- direction

\( \beta \) = resistance exponent = 5/3

\( \frac{\partial s}{\partial t} \bigg|_t \) = value of model state variable derivative at time t

\( \Phi \) = total soil porosity

\( \theta_e \) = effective soil porosity = \((\Phi - \theta_r)\)

\( \theta_r \) = residual soil moisture content
Chapter I. Introduction

Section 1.1 Overview

While dams provide the ability to control the flow of fresh water and function to simplify our lives in many ways, they also pose an inherent and inevitable threat to the environment and to public safety. Since the creation of the first dams, dams have been failing due to unpredictable environmental conditions, poor engineering, or improper management. Unfortunately, when dams fail they often do so catastrophically because of the large amount of potential energy involved. Many engineering efforts have been made to reduce the potential hazard of dams as well as to provide emergency action plans for the event of a dam failure. Modeling the dam failure and overtopping processes and routing flood waves downstream can provide basic information about flood events that can be beneficial in dam engineering, emergency action planning, and floodplain management.

Due to the complex nature of the hydraulics involved with dam overtopping and large flood routing, much of the computer modeling in these areas has been done with one-dimensional models. However, in recent years there has been considerable progress in model code development, computing speed and capability and available elevation, vegetation, soil type, and land use data. The progress in these areas has led to much interest in multi-dimensional modeling of dam failure, overtopping, and flood routing as these events are certainly multi-dimensional in nature. To date there have been several explicit dam failure models developed which simulate the dam failure mechanism and localized effects (Wahl 1998, 2010). Watershed scale models can also be very valuable in
the analysis of dam failure, overtopping and flood routing by simulating the larger scale system influences on a reservoir and downstream effects of failure and overtopping events.

1.1.1 Dam Breach and Overtopping (The Problem)

As dams pose a serious threat to residents, businesses, infrastructure, landowners, crops, etc. downstream of them, it has always been important to analyze the causes and results of dam failure and dam overtopping. It is also important to understand the effect that reservoirs can have on large precipitation events within a watershed, as they can have the ability to contain upstream flooding and attenuate total peak discharge. There are currently about 80,000 dams listed in the U.S. national inventory (Altinakar 2008). 81% of these are earthen dams, and 1,595 are considered a significant hazard to a city downstream. Dam failures have proven to be quite deadly, destructive, and costly.

Table 1.1: Selected dam failures (Association of Dam Safety Officials)

<table>
<thead>
<tr>
<th>Date</th>
<th>Name</th>
<th>Fatalities</th>
<th>Estimated Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>May 6, 1874</td>
<td>Mill River Dam, Massachusetts</td>
<td>139</td>
<td></td>
</tr>
<tr>
<td>May 31, 1889</td>
<td>South Fork Dam, Massachusetts</td>
<td>&gt;2,200</td>
<td></td>
</tr>
<tr>
<td>Feb. 26, 1972</td>
<td>Buffalo Creek Valley, West Virginia</td>
<td>125</td>
<td>$400 million</td>
</tr>
<tr>
<td>June 9, 1972</td>
<td>Canyon Lake Dam, South Dakota</td>
<td>Between 33 and 237</td>
<td>$60 million</td>
</tr>
<tr>
<td>June 5, 1976</td>
<td>Teton Dam, Idaho</td>
<td>11</td>
<td>$1 billion</td>
</tr>
<tr>
<td>June 19, 1977</td>
<td>Laurel Run Dam, Pennsylvania</td>
<td>&gt;40</td>
<td>$5.3 million</td>
</tr>
<tr>
<td>Nov. 5, 1977</td>
<td>Kelly Barnes Dam, Georgia</td>
<td>39</td>
<td>$2.5 million</td>
</tr>
</tbody>
</table>
Historically the vast majority of dam failures have been caused by overtopping. Dam overtopping can also cause a flood pulse downstream of a dam without the dam failing due to the stage discharge relationship of the reservoir. Dam overtopping and dam failure are very difficult processes to understand, predict, analyze, or model due to the inherently complex and contextual nature of the overtopping and failure processes and the lack of existing data relevant to dam failure.

![Image](NPDP.png)

**Figure 1.1:** Relative number of dam failures due to a variety of mechanisms (Association of Dam Safety Officials)

At the watershed scale there are several sub-processes that make up the hydrologic response to precipitation induced flooding when a dam is involved. Each separate process of a dam overtopping or dam failure scenario (precipitation, geotechnical failure, or flood routing) can be analyzed separately or the total process analyzed as one event. Analyses of particular process aspects of these events can be especially beneficial when combined with
other similarly developed analyses to create an understanding of the entire process and consequence of these events. Processes such as the retention of flood flows by reservoirs with available capacity and the downstream routing of flows that overtop a dam lend themselves well to watershed scale numerical modeling analysis techniques.

1.1.2 Modeling Dam Overtopping and Flood Routing

Section 1.2 Objectives

The objectives of this research are as follows:

1). Ascertain the necessary model time step required to maintain numerical stability for routing a large range, in peak discharge magnitude, of point source hydrographs.

2). Simulate the inundation of the flood plain below a reservoir due to a dam failure by introducing flood wave simulating hydrographs into the watershed at a point. Map the areal extent of the downstream flooding. Quantify the areal extent of flood plain inundation. Create enhanced graphical and animation representations of simulation results to improve interpretation and visualization of simulation results.

3). Simulate the dam overtopping process as the result of extreme precipitation events. Quantify the attenuation of flood hydrograph peak discharge at the outlet of a watershed due to upstream dams.
Chapter II. Literature Review

Section 2.1 Dam Breach Modeling Techniques Overview

Dam failure modeling can generally be sorted into three categories of analysis techniques. The first technique is regression analysis utilizing the available dam failure data. This data includes outflow hydrograph data and dam geometry. The second category involves analytically modeling the dam failure process by characterizing the physical processes involved with the failure process to make predictions. The third technique is numerically modeling dam failure, overtopping, and flood wave routing with a computer model.

Dam failure and overtopping computer modeling can essentially be categorized into two major types of models, those that explicitly model the dam failure mechanism and outflow hydrograph and those that model the watershed scale hydrology and hydraulics in order to quantify the amount of water available to a reservoir and then route an outflow hydrograph from a dam. Coupling of these two types of models can also be done to simulate the entire process at a watershed scale and localized scale.

Presented in the following sections are overviews of the current and past research with each of the aforementioned techniques and examples thereof. This review is not intended to be comprehensive, but rather a general picture of the available dam failure, overtopping, and flood wave routing modeling techniques will be presented.

2.1.1 Dam Breach Empirical Models

Although there have been thousands of man-made and natural dam failures, there is not an abundance of data available concerning dam failure events due either to a lack of
downstream gaging or to downstream gages being compromised during the flood event. However, work has been done to compile the available data in order to estimate flood characteristic parameters as a function of dam geometry and reservoir geometry parameters by regression analysis. A general description of the research that has been done in dam failure regression analysis will be presented here. Additionally, the manner by which these types of empirical relationships can be applied to modeling with TREX will be discussed in Chapter V.

The magnitude of the peak discharge from a dam failure and the time to peak discharge are two important parameters due to their direct relation to downstream floodplain management. Several researchers such as Froehlich, Pierce and Singh over the past few decades have compiled both measured and estimated flood hydrograph data and, by regression analysis, related the peak discharge and time to peak discharge to various geometric characteristics of the failed dams or associated reservoirs. Parameters such as dam crest height, dam crest width, dam crest length, and reservoir volume have been used for these regression analyses. Thornton et al. 2011 summarized the resulting empirical functions of many of these analyses and also presented a multivariate regression analysis utilizing the data sets that were used for the regression analyses. Table 2.1 shows the compiled summary of dam failure empirical relationships.
Table 2.1: Summary of dam breach hydrograph empirical relationships (Thornton et al. 2011)

<table>
<thead>
<tr>
<th>Investigator</th>
<th>Type</th>
<th>$R^2$</th>
<th>Number of case studies</th>
<th>Real</th>
<th>Simulated</th>
<th>Equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Height of water equations</td>
<td>Best fit</td>
<td>0.790p</td>
<td>13</td>
<td>6</td>
<td>13</td>
<td>$Q_p = 1.268(H_w + 0.3)^{2.5}$</td>
</tr>
<tr>
<td>Soil Conservation Service (SCS) (1981) for dams &gt; 31.4 m</td>
<td>Envelopeb</td>
<td>Not available</td>
<td>21</td>
<td>8</td>
<td>21</td>
<td>$Q_p = 16.66H_w^{1.85}$</td>
</tr>
<tr>
<td>U.S. Bureau of Reclamation (1982)</td>
<td>Envelope</td>
<td>0.724</td>
<td>72</td>
<td>72</td>
<td>72</td>
<td>$Q_p = 13.46H_w^{0.89}$</td>
</tr>
<tr>
<td>Singh and Snorrasen (1982)</td>
<td>Best fit</td>
<td>0.633</td>
<td>72</td>
<td>72</td>
<td>72</td>
<td>$Q_p = 0.784H_w^{1.66}$</td>
</tr>
<tr>
<td>Pierce et al. (2010)—linear</td>
<td>Best fit</td>
<td>0.640</td>
<td>72</td>
<td>72</td>
<td>72</td>
<td>$Q_p = 2.325 lnH_w^{0.95}$</td>
</tr>
<tr>
<td>Pierce et al. (2010)—curvilinear</td>
<td>Best fit</td>
<td>0.918</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>$Q_p = 1.776S^{0.87}$</td>
</tr>
<tr>
<td>Singh and Snorrasen (1984)</td>
<td>Best fit</td>
<td>0.836</td>
<td>29</td>
<td>29</td>
<td>29</td>
<td>$Q_p = 0.721V_e^{0.53}$</td>
</tr>
<tr>
<td>Evans (1986)</td>
<td>Best fit</td>
<td>0.805</td>
<td>87</td>
<td>87</td>
<td>87</td>
<td>$Q_p = 0.08919(V_e)^{0.733}$</td>
</tr>
<tr>
<td>Pierce et al. (2010)</td>
<td>Envelope</td>
<td>Not Available</td>
<td>6</td>
<td>6</td>
<td>6</td>
<td>$Q_p = 1.205(V_e - H_w)^{0.48}$</td>
</tr>
<tr>
<td>Height of water and storage equations</td>
<td>Best fit</td>
<td>0.788</td>
<td>23</td>
<td>23</td>
<td>23</td>
<td>$Q_p = 1.154(V_e - H_w)^{0.412}$</td>
</tr>
<tr>
<td>Hagen (1982)</td>
<td>Envelope</td>
<td>0.156</td>
<td>23</td>
<td>23</td>
<td>23</td>
<td>$Q_p = 3.85(V_e - H_w)^{0.411}$</td>
</tr>
<tr>
<td>MacDonald and Langridge-Monopolis (1984)</td>
<td>Best fit</td>
<td>0.745</td>
<td>31</td>
<td>31</td>
<td>31</td>
<td>$Q_p = 0.763(V_e - H_w)^{0.42}$</td>
</tr>
<tr>
<td>Costa (1985)</td>
<td>Best fit</td>
<td>0.844</td>
<td>87</td>
<td>87</td>
<td>87</td>
<td>$Q_p = 0.01764V_e^{-0.006}$</td>
</tr>
<tr>
<td>Pierce et al. (2010)</td>
<td>Best fit</td>
<td>0.934</td>
<td>22</td>
<td>22</td>
<td>22</td>
<td>$Q_p = 0.607(V_e)^{0.265}H_w^{2.74}$</td>
</tr>
<tr>
<td>Pierce et al. (2010)</td>
<td>Best fit</td>
<td>0.850</td>
<td>87</td>
<td>87</td>
<td>87</td>
<td>$Q_p = 0.038(V_e + 0.25H_w)^{1.98}$</td>
</tr>
</tbody>
</table>

¹This $R^2$ value was calculated using a portion of the writer’s original data set.
²Wahls (1998) suggested that this is an enveloping equation even though three data points plot slightly above the curve.
³This $R^2$ value was calculated without the five concrete and masonry dams included in the writer’s original data set.

Figure 2.1: Dam failure data sets (Thornton et al. 2011)

The following relationships are the multivariate regression equations that were developed for the peak discharge from a dam breach:

$$Q_p = 0.863V_x^{0.335}H_w^{1.833}W_{ave}^{-0.633}$$ (2.1)
In Equations 2.1 and 2.2:

\[ Q_p = 0.012 \left( V_s^{0.493} H_d^{1.205} L^{0.226} \right) \]  

(2.2)

In Equations 2.1 and 2.2:

- \( V_s \) = volume of water behind the dam
- \( H_d \) = dam crest height
- \( W_{ave} \) = average embankment width (perpendicular to the crest)
- \( L \) = embankment length (crest length)

It was determined that when the number of pertinent dam characteristic variables increased from one to three as in these equations, the coefficient of variation increased slightly and the mean predicted error and the uncertainty bandwidth decreased (Thornton 2011).

Similar regression analyses have been done to develop equations for the time to failure of a breach outflow. Figure 2.2 was taken from the 1998 Department of the Interior Bureau of Reclamation Dam Safety Office report entitled “Prediction of Embankment Dam Breach Parameters”. This figure details predicted versus observed time of failure values as determined by Froehlich 1995, Von Thun and Gillette 1990, MacDonald and Langridge-Monopolis 1984, and Reclamation 1988.

The relationships that have been developed by regression analyses of these data sets are tools for rough estimation of flood characteristics which can be helpful in emergency response and flood plain management. These relationships can also be used in conjunction with computer models. These methods will be discussed in chapter V.
2.1.2 Dam Break Analytical Models

While the water flow and erosional physical processes involved in dam failure are well known, they are still difficult to analytically model and quantify due to complex turbulence and rapidly varying characteristics. However, several analytical models have
been developed that determine the discharge from a dam breach from mathematical formulations of the physics of the breach process.

Cristofano, in 1965, related the erosion of a breach channel to the discharge though the breach using the shear strength of the dam material and the force of the flowing water (Wahl 2010). Several assumptions were made about the shape of the breach and an empirical coefficient was used to calibrate the model (Wahl 2010). Walder and O’Connor, in 1997, developed a model for the peak discharge from a breach as a function of the material erosion rate, the reservoir size, a breach shape parameter, the breach side slope angle, a reservoir shape factor, and the breach depth-to-dam height ratio (Wahl 2010). The following “benchmark case” relationships were developed for the peak discharge \( Q_p \) from a natural or constructed earthen dam breach and the time to peak discharge \( t_p \) (Walder and O’Connor 1997).

\[
Q_p = 1.51 \left( g \frac{h_d^{5/2}}{V_s} \right)^{0.06} \left( \frac{k_b V_s}{h_d^{2}} \right)^{0.94} \approx 1.24 \left( \frac{V_s}{(g h_d^{2})^{1/2}} \right)^{1/3} \text{ for } \left( \frac{k_b}{(g h_d^{2})^{1/2}} \right) \frac{V_s}{h_d^{3/2}} \leq 0.6
\]

\[
Q_p = 1.94 \left( g \frac{1/2}{h_d^{5/2}} \right)^{1/4} \left( \frac{D_c}{h_d} \right)^{1/4} \approx \frac{h_d}{k_b} \text{ for } \left( \frac{k_b}{(g h_d^{2})^{1/2}} \right) \frac{V_s}{h_d^{3/2}} \gg 1
\]

In Equations 2.3 and 2.4:
- \( g \) = gravitational acceleration
- \( h_d \) = water level drop in reservoir
- \( k_b \) = mean erosion rate of the breach
- \( V_s \) = volume of water stored behind the dam
- \( D_c \) = dam crest height

The first equation applies to reservoirs where the volume stored to dam height ratio is small and the second equation applies to reservoirs where the volume stored to dam height ratio is large.
height ratio is large. These formulations apply to average reservoir conditions for all parameters that are not present in the equations. This method recognizes the difference in dam failure processes between large and small reservoirs. Table 2.2 summarizes several popular physically based dam breach models that have been developed.

Table 2.3: Physically-based embankment breach parameters (Wahl 1998)

<table>
<thead>
<tr>
<th>Model and Year</th>
<th>Sediment Transport</th>
<th>Breach Morphology</th>
<th>Parameters</th>
<th>Other Features</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cristofano (1965)</td>
<td>Empirical formula</td>
<td>Constant breach width</td>
<td>Angle of repose</td>
<td></td>
</tr>
<tr>
<td>Harris and Wagner (1967); BRDAM (Brown and Rogers, 1977)</td>
<td>Schoklitsch formula</td>
<td>Parabolic breach shape</td>
<td>Breach, dimensions, sediments</td>
<td></td>
</tr>
<tr>
<td>DAMBRK (Fread, 1977)</td>
<td>Linear predetermined erosion</td>
<td>Rectangular, triangular, or trapezoidal</td>
<td>Breach dimensions, others</td>
<td>Tailwater effects</td>
</tr>
<tr>
<td>Lou (1981); Ponce and Tsivoglou (1981)</td>
<td>Meyer-Peter and Muller formula</td>
<td>Regime type relation</td>
<td>Critical shear stress, sediment</td>
<td>Tailwater effects</td>
</tr>
<tr>
<td>BREACH (Fread 1988)</td>
<td>Meyer-Peter and Muller modified by Smart</td>
<td>Rectangular, triangular, or trapezoidal</td>
<td>Critical shear stress, sediment</td>
<td>Tailwater effects; dry slope stability</td>
</tr>
<tr>
<td>BEED (Singh and Scarlakos, 1985)</td>
<td>Einstein- Brown formula</td>
<td>Rectangular or trapezoidal</td>
<td>Sediments, others</td>
<td>Tailwater effects, saturated slope stability</td>
</tr>
<tr>
<td>FLOW SIM 1 and FLOW SIM 2 (Bodine, undated)</td>
<td>Linear predetermined erosion; Schoklitsch formula option</td>
<td>Rectangular, triangular, or trapezoidal</td>
<td>Breach dimensions, sediments</td>
<td></td>
</tr>
</tbody>
</table>

2.1.3 Dam Breach Computer Models

The National Weather Service (NWS) dam-break forecasting model FLDWAV was developed by D. L. Fread to model the dam breach process and the downstream flooding process. FLDWAV took over for the popular DAMBRK model which has been used since the
nineteen seventies (Fread 1984, 1993). FLDWAV utilizes a finite-difference numerical method to solve the complete one dimensional Saint Venant equations for unsteady flow. The model will compute the outflow hydrograph from a dam resulting from spillway flow, overtopping, and/or dam breach and then route the flood wave downstream. Internal boundary conditions can be input to represent man-made control structures such as dams, weirs, and bridges. The flow may be subcritical, supercritical, or mixed and can also vary from Newtonian to non-Newtonian (Fread and Lewis 1998).

The BREACH dam breach model predicts the outflow hydrograph from an earthen dam using a physically based approach which takes into account various geometric, geotechnical, erosional, and flow characteristics (Fread 1988). The model uses information about the constituent materials of a dam along with the Meyer-Peter and Müller sediment transport equation and a quasi-steady uniform flow (manning equation) to define the breach opening evolution in time. Subsequently the outflow hydrograph can be determined. The BREACH model code is free.

The United States Army Corps of Engineers (USACE) Hydrologic Engineering Center (HEC) developed the HEC-RAS Hydraulic channel flow model as part of their suite of hydrologic and hydraulic modeling tools (Brunner 2010). While primarily used as a flow routing model, a dam breach module has been added to the model to simulate the breach process. HEC-RAS can simulate steady or unsteady one-dimensional flow by solving the full one dimensional Saint-Venant equations. Also subcritical, supercritical, or mixed flow regimes can be simulated.
2.1.4 Watershed Computer Models

Over the past several decades, many watershed scale computer models have been developed within government agencies, academia, and the private sector. Watershed models are often categorized into lumped parameter, semi-distributed parameter, and distributed parameter models. Lump parameter models are those which assign one parameter value to the whole watershed. Semi-distributed models are those which distribute parameter values by sub-catchments within a watershed. Distributed parameter models divide a watershed into a grid of cells and assign a parameter value to each cell within the watershed domain. Several in-depth comparative reviews of watershed models have been done. The World Meteorological Organization (WMO) has sponsored comparative studies of watershed models in 1975, 1986, and 1992. Singh et al. have written comparisons as well (Singh et al. 2002). The National Weather Service (NWS) sponsored a review of distributed models called the distributed model inter-comparison project (DIMP) (Smith et al. 2004). In the interest of providing context for the research presented here regarding modeling with the TREX watershed model, several popular models will be described here. An inter-comparison table taken from Singh et al. 2002 is presented in Appendix 2.0. A more detailed review of the TREX model will be presented in Chapter III.

The United States Army Corps of Engineers (USACE) has developed a series of lumped parameter watershed models. The most recent version is the Hydrologic Engineering Center (HEC) Hydrologic Modeling System (HEC-HMS) (Feldman 2010). This model simulates watershed scale processes using empirical equations. This model and similar lumped parameter models are simple to use and require far less set up time and
field data to run than distributed models. In many cases they can be as accurate as a more sophisticated physically based model. However, they do not represent the runoff characteristics of complex watersheds which have highly varied soil types or land uses as well as distributed parameter models. They will not provide information about the distribution of flow within a watershed. Also they always require calibration, which essentially limits their utility to cases where calibration and validation data are available.

An example of a semi-distributed parameter model is the Hydrologic Simulation Program-Fortran (HSPF) (Bicknell et al. 1997). This model has its roots in one of the oldest watershed models, the Stanford Watershed Model (Crawford and Linsley, 1966). This model simulates many hydrologic, sediment transport, and chemical transport processes. The hydrologic processes are represented as stored water and flow is routed between storages (Velleux et al. 2010). Flow is simulated with the one-dimensional kinematic wave approximation of the Saint Venant equation.

The Kinematic Runoff and Erosion (KINEROS) is another example of a semi-distributed parameter model (Woolhiser et al. 1990). This model is an example of an “open book” model whereby a watershed is represented by planes which route flow into channels. KINEROS simulates rainfall, interception, infiltration, surface runoff, and erosion. Flow is calculated by the one-dimensional kinematic wave approximation of the Saint Venant equation.

The Soil and Water Assessment Tool (SWAT) is another example of a physically based semi-distributed parameter model which simulates rainfall, infiltration, surface flow, groundwater flow, and transmission losses (Neistch et al. 2002). SWAT has been linked
with the Arc/Info geographic information system (GIS) (Velleux et al. 2010). All three of these semi-distributed parameter models have publicly available source code.

System Hydrologique European Fortran (SHETRAN) is a fully-distributed parameter, physically based model which simulates interception, infiltration, surface runoff, groundwater flow, evapotranspiration, sediment transport, and chemical transport (Ewen et al. 2000). Surface flow is calculated with the diffusive wave approximation of the Saint Venant equation. This model is two-dimensional in the overland plane and one dimensional in channels. Groundwater flow is three-dimensional. While SHETRAN is not commercially available, there is a commercially available package called MIKE SHE (DHI 2005).

FLO-2D is a two-dimensional physically based model which simulates rainfall, surface flow, interception, and infiltration (O’Brien 2006). FLO-2D uses the full dynamic wave Saint-Venant equation to route flow in two dimensions. This software is commercially available and there is a free basic version.

Several features of a computer model are necessary or highly desirable when modeling dam overtopping and large magnitude flood events at the watershed scale. A model must be a fully distributed parameter type in order to analyze the interactions between the floodplain and the channel and to map the distribution of flow within a watershed in time. Floodplain interactions are complex due to highly varied roughness and many possible flow directions. Fully distributed models best capture this detail. Also location specific events like overtopping and dam failure must be modeled with a fully distributed model in order to accurately represent the localized detail at a dam site. A model should also route flow in two dimensions in the flood plain. Large scale flood flows
are very multi-dimensional in nature as the flows are not confined by channel walls. Modeling floods that originate from a point within a watershed requires a model that is capable of accepting a user defined point source hydrograph as input. The incorporation of a GIS program into the pre-processing of model input data and post-processing of model calculated, distributed flow depths and velocities is crucial for this type of modeling. It allows for easy modification of watershed elevations for dam representations. It also provides a vehicle for visually interpreting model outputs in the form of maps and animations.

The TREX model is a fully distributed parameter, physically based, two dimensional model that is easily integrated with a GIS program such as the Environmental Systems Research Institute (ESRI) ArcGIS suite of GIS tools. TREX is also an open source model that is free to the public. For these reasons TREX is well suited to watershed scale modeling of dam overtopping and flood routing. These attributes and other aspects of the TREX model are discussed in chapter III.
Chapter III. The Two-Dimensional Runoff Erosion and Export Model

Section 3.1 TREX Conceptual Model

The Two-Dimensional Runoff Erosion and Export (TREX) watershed model is composed of three distinct components which are hierarchical in their dependence on one another. The first and most basic component of the model is the hydrologic group of processes which simulates precipitation, infiltration, storage, and overland and channel flow. These processes are controlled by the governing equations of water flow and input parameters that describe the geography and roughness of the watershed, namely the Digital Elevation Model and land use types. The second component is the sediment transport group of processes which governs aggradation, degradation, and sediment advection in the overland plane and in the channel. These processes are all dependent on the hydrologic governing equations and various soil characteristic input parameters. The third component controls the transport and fate of chemicals within the watershed. The constituent processes of this component are dependent on those of the first two model components.

The hydrologic model component can be run alone, or sediment transport can be modeled with hydrology, or chemical fate and sediment transport can be modeled with hydrology. Only the hydrologic process descriptions and governing equations will be detailed here, as the other two model components were not utilized for the dam failure and dam overtopping simulations presented.
Section 3.2  Hydrologic Process Descriptions

The main hydrologic processes incorporated into the hydrologic model component are precipitation and interception, infiltration and transmission loss, surface storage, and overland and channel flow (Velleux 2005). Much of the notation and description presented for the hydrologic sub-model are taken from the TREX user manual (Velleux et al. 2011).

3.2.1 Precipitation and Interception

The precipitation that effectively reaches the land or water surface can be represented as a depth or volume of water. The representation of continuity which reflects this is the following:
\[ \frac{\partial V_g}{\partial t} = i_g A_s \]  

(3.1)

In Equation 3.1:  
\( V_g \) = gross precipitation water volume  
\( i_g \) = gross precipitation rate  
\( A_s \) = surface area over which the precipitation occurs  
\( t \) = time

Surface vegetation effectively reduces the total amount of water available for infiltration or run off by trapping water by surface tension with the foliage. Intercepted water can be stored by the vegetation or can evaporate. Intercepted precipitation can be represented as a depth or volume.

\[ V_i = (S_i + E t_R) A_s \]  

(3.2)

The net precipitation available for infiltration or run off can then be represented as the gross precipitation volume minus the intercepted volume.

\[ V_n = V_g - V_i \]  

(3.3)

In Equations 3.2 and 3.3:  
\( V_i \) = interception volume  
\( S_i \) = interception capacity of projected canopy per unit area  
\( E \) = evaporation rate  
\( t_R \) = precipitation duration  
\( V_n \) = net precipitation
When gross precipitation volume is greater than the intercepted volume, then the excess precipitation volume can be represented as a net effective precipitation rate as follows:

\[
i_n = \frac{1}{A_i} \frac{\partial V_n}{\partial t}
\]

(3.4)

In Equation 3.4: \(i_n\) = net effective precipitation rate

### 3.2.2 Infiltration and Transmission Loss

Infiltration is the transport of surface water into the subsurface due to gravity and capillary action. Many parameters affect a soil’s ability to convey water such as hydraulic conductivity, capillary suction head, and degree of saturation. The Green and Ampt infiltration process description is incorporated by TREX where any infiltrated water is considered to be a loss from the surface water. This relationship assumes that a sharp wetting front exists at the interface of the infiltration zone and the initial water content. When the pressure head due to surface ponding is neglected, that is to say that it is much smaller than the suction head, the Green and Ampt relationship can be expressed as the following (Julien, 2002):

\[
f = K_h \left(1 + \frac{H_c (1 - S_c) \theta_e}{F}\right)
\]

(3.5)

In Equation 3.5: \(f\) = infiltration rate

\(K_h\) = effective hydraulic conductivity

\(H_c\) = capillary pressure (suction) head at the wetting front

\(\theta_e\) = effective soil porosity = \((\Phi - \theta_r)\)

\(\Phi\) = total soil porosity
Water can infiltrate in channels similarly to how it does in the overland plane.

Transmission loss in channels is also modeled with the Green and Ampt relationship in TREX. However ponded surface water and the associated hydrostatic pressure head are accounted for. The transmission rate can be expressed as the following:

\[ t_i = K_h \left( 1 + \frac{(H_w + H_c)(1 - S_e)\theta_r}{T} \right) \]  

(3.6)

In Equation 3.6:  
- \( t_i \) = transmission loss rate  
- \( K_h \) = effective hydraulic conductivity  
- \( H_w \) = hydrostatic pressure head (depth of water in channel)  
- \( H_c \) = capillary pressure (suction) head at the wetting front  
- \( \theta_e \) = effective soil porosity = \((\Phi - \theta_r)\)  
- \( \Phi \) = total soil porosity  
- \( \theta_r \) = residual soil moisture content  
- \( S_e \) = effective sediment saturation  
- \( T \) = cumulative (total) depth of water transported by transmission loss

### 3.2.3 Storage

Water that is stored in surface depressions both in the overland plane and within channels is represented within TREX as an equivalent total volume or when normalized by the raster cell area, as a depth. A threshold depth in surface depressions creates a
condition for the initiation of water flow. The stored water in overland and channel cells is subject to infiltration and evaporation.

### 3.2.3 Overland and Channel Flow

Water flow will occur in overland and channel cells when the surface water depth exceeds the depression storage threshold depth. Flow can generally be described by conservation of mass (continuity) and conservation of momentum. Within TREX water can flow in two dimensions. The two-dimensional (vertically integrated) equation of continuity for gradually varied flow in the overland plane in rectangular coordinates is the following (Julien et al. 1995; Julien, 2002):

$$\frac{\partial h}{\partial t} + \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} = i_n - f + W = i_e \tag{3.7}$$

In Equation 3.7:

- \( h \) = surface water depth
- \( q_x, q_y \) = unit discharge in the x- or y- direction = \( Q_x/B_x, Q_y/B_y \)
- \( Q_x, Q_y \) = flow in the x- or y- direction
- \( B_x, B_y \) = flow width in the x- or y- direction
- \( i_n \) = net effective precipitation rate
- \( f \) = infiltration rate
- \( W \) = unit discharge from/to a point source/sink
- \( i_e \) = excess precipitation rate

The momentum of overland and channel flow can be represented by the Saint-Venant equations. These equations can be simplified to the diffusive wave approximation if the relatively small terms that describe the local and convective acceleration are neglected (Julien et al. 1995; Julien, 2002):
In Equations 3.8 and 3.9:

\[ S_{fx} = S_{0x} - \frac{\partial h}{\partial x} \]  
\[ S_{fy} = S_{0y} - \frac{\partial h}{\partial y} \]

In Equations 3.8 and 3.9:

\[ S_{fx}, S_{fy} = \text{friction slope in the x- or y- direction} \]
\[ S_{0x}, S_{0y} = \text{ground surface slope in the x- or y- direction} \]

To solve continuity and momentum equations for flow in the overland plane, five hydraulic variables can be defined which describe flow resistance in terms of a depth-discharge relationship. Flow resistance can be described by the manning equation, assuming that is turbulent. The depth discharge relationships for two-dimensional flow in the overland plane are the following (Julien et al. 1995; Julien, 2002):

\[ q_x = \alpha_x h^\beta \]  
\[ q_y = \alpha_y h^\beta \]  
\[ \alpha_x = \frac{S_{fx}^{1/2}}{n} \]  
\[ \alpha_y = \frac{S_{fy}^{1/2}}{n} \]

In Equations 3.10, 3.11, 3.12 and 3.13:

\[ \alpha_x, \alpha_y = \text{resistance coefficient} \]

for flow in the x- or y- direction

\[ S_{fx}, S_{fy} = \text{friction slope in the x- or y- direction} \]

\[ \beta = \text{resistance exponent} = 5/3 \]
If channel flow is simplified to a one-dimensional approximation (vertically and laterally integrated) in the direction parallel to the channel thalweg, the equation for continuity can be expressed as follows (Julien et al. 1995; Julien, 2002):

\[
\frac{\partial A_c}{\partial t} + \frac{\partial Q}{\partial x} = q_l
\]

(3.14)

In Equation 3.14:
- \(A_c\) = cross sectional area of flow
- \(Q\) = total discharge
- \(q_l\) = lateral unit discharge (into or out of the channel)

The diffusive wave approximation of the full Saint-Venant equation can once again be used to describe conservation of momentum for one-dimensional channel flow, assuming that the local and convective acceleration terms of the Saint-Venant equations are relatively small and can be neglected (Equations 3.8 and 3.9). The Manning equation to represent channel flow resistance is the following (Julien et al. 1995; Julien, 2002):

\[
Q = \frac{1}{n} A_c R_h^{\frac{2}{3}} S_f^{\frac{1}{2}}
\]

(3.15)

In Equation 3.15:
- \(Q\) = total discharge
- \(A_c\) = cross sectional area of flow
- \(R_h\) = hydraulic radius of flow = \(A_c/P_c\)
- \(P_c\) = wetted perimeter of channel flow
- \(n\) = Manning roughness coefficient
- \(S_f\) = friction slope
Section 3.3  Numerical Method

The TREX model solves the governing equations for all of the state variables involved with the hydrologic, sediment transport, and chemical transport sub-models. The model uses a finite difference, first order numerical integration scheme to solve the flow equations for every raster cell in the watershed domain as individual control volumes. Euler’s method for numerical integration is used as the technique to solve the governing equations at every time step.

\[
\left. s \right|_{t+dt} = s \left|_t \right. + \left. \frac{\partial s}{\partial t} \right|_t \, dt
\]

(3.16)

In Equation 3.16:  
\[ s \left|_{t+dt} \right. = \text{value of the model state variable at time } t + dt \]
\[ s \left|_t \right. = \text{value of the model state variable at time } t \]
\[ \left. \frac{\partial s}{\partial t} \right|_t = \text{value of model state variable derivative at time } t \]
\[ dt = \text{time step for numerical integration} \]

This numerical method requires that model stability is highly dependent on the magnitude of the simulation time step, \( dt \). The model accepts as input a series of user specified time steps, or a model option can be selected whereby the Courant-Freidrichs-Lewy (CFL) condition is employed by the model to determine the maximum stable time step at each simulated iteration (Velleux et al. 2011).

\[
\frac{u \, dt}{dx} \leq C
\]

(3.17)

In Equation 3.17:  
\( c = \text{celerity} \)
\( dt = \text{model time step} \)
\( dx \quad = \) modeled raster cell size

\( C \quad = \) Courant number
Chapter IV. California Gulch Model Configuration

Section 4.1 Overview and Site Description

California gulch is a watershed which drains into the upper Arkansas River near the town of Leadville in central Colorado (Figure 4.1).

![Map of California Gulch and Leadville](image)

Figure 4.1: Study site location, California Gulch, Colorado (Velleux 2005)

The California Gulch watershed encompasses most of the city of Leadville and the uplands east of the city. California Gulch has several tributaries, the largest of which is
Stray Horse Gulch which joins California Gulch within the city of Leadville (Figures 4.1 and 4.2).

Figure 4.2: California Gulch watershed and Leadville Colorado

A portion of the watershed is urbanized and more impervious than the rest of the drainage area. The headwaters of the watershed are at and above tree line and much of this region was heavily mined in the late 1800’s and early 1900’s. The hard rock mining techniques of this era have led to a reduction in vegetation and considerable sediment instability and heavy metal contaminant drainage. This change in the land use has significantly changed the hydrology and ecology of the area and as such, the Environmental Protection Agency (EPA) established a superfund project site in California Gulch and Stray Horse Gulch. Several flow paths have been altered by diversions and settling ponds. Much of the rest of
the watershed is evergreen forested. Figure 4.7 shows the full detail of the land use representation.

Section 4.3 Digital Elevation Model

The area of California Gulch is 30.6 km². The elevation within the watershed varies between 3654 meters and 2910 meters (Figure 4.3). A Digital Elevation Model (DEM) was created for California Gulch with Geographic Information System (GIS) software and elevation data from the United States Geological Survey (USGS). 30 meter by 30 meter resolution elevation data was used to create the grid elevation representation of the watershed. The DEM contains 34,002 cells.
Figure 4.3: California Gulch digital elevation model

Slope and aspect maps were also created to delineate the watershed and create a flow network during the DEM processing of the watershed. These processes were utilized during the original model set up creation for the California Gulch watershed.
Figure 4.4: California Gulch aspect map

Figure 4.5: California Gulch slope map
A stream network was created with 25 links and 1395 nodes. 42 km of total stream length was created to distinguish between channel flow and overland flow.

Figure 4.6: California Gulch link map

Section 4.4  Land Use

Land use data were also obtained from the USGS. A land use map was created to represent the surface roughness of the watershed for model calculations. Values for parameters such as ground cover factor, surface roughness, vegetative interception depth, grain size, and erodibility were assigned to each land use type (Velleux 2005).
Section 4.5  Soil and Sediment Types

Soil survey data was obtained from the U.S. Department of Agriculture (USDA) and the Natural Resources Conservation Service (NRCS). These data provided characterizations of the soils of the watershed such as hydraulic conductivity, porosity, and grain size distribution. Additional soil data was acquired from EPA superfund project reports. Values for parameters such as grain size, hydraulic conductivity, and porosity

Figure 4.7: California Gulch land use type map
were assigned to each soil type (Velleux 2005).

![California Gulch Soil Type Map](image)

**Figure 4.8: California Gulch soil type map**

**Section 4.6  Overview of Work Done at California Gulch**

Much work has been done in past years collecting a comprehensive dataset which has been compiled to develop the California Gulch TREX model set up. Data collected for the EPA, Resurrection Mining Company, American Smelting and Refining Company (ASARCO), Denver and Rio Grande Railroad Company, and Colorado Department of Public Health and Environment (CDPHE) was used for this model set up. Additionally, data from
the USGS and the USDA was extracted from databases for use in the model setup. While much of this data collected was for the part of the model setup which characterizes the sediment and chemical transport of the watershed, the data pertaining to soil type, land use, elevation, soil moisture, and precipitation was integral to the model simulations preformed for this analysis.

Figure 4.9: California Gulch gaging stations (Velleux 2005)

Section 4.7 Calibration and Validation

The calibration event used for the California Gulch model set up was on June 12-23, 2003 (Velleux 2005). The validation event used was on September 5 – 8, 2003. Figure 4.9 shows the gaging station locations within the California Gulch watershed and Figures 4.10 and 4.11 show the results of the calibration and validation simulations. The details about
the model performance are available from Velleux 2005.

Figure 4.10: California Gulch hydrologic calibration (Velleux 2005)
Figure 4.11: California Gulch hydrologic validation (Velleux 2005)
Chapter V.  Flood Routing, Point Source Simulation

Section 5.1  Overview of Work

A point source hydrograph can be inserted into the DEM of a TREX simulation at a specified raster cell. In this way flood routing can be done in order to analyze the characteristics of the flood progression through a watershed. Particularly the inundation of the flood plain as a function of time and downstream distance can be simulated.

**Triangular Point Source Input Hydrograph**

![Triangular Point Source Input Hydrograph](image)

*Figure 5.1: Typical approximated point source hydrograph*

The outflow from a dam failure can be routed within the TREX model without simulating the localized failure mechanism. A user defined hydrograph can be introduced to a point in the watershed. In this way a known dam failure hydrograph can be routed downstream and through the flood plain. Also a dam failure can be simulated with an
empirical, an analytical, or an explicit dam breach numerical model and the determined outflow can be input into TREX to be routed through the watershed.

Section 5.2 Model Stability and Time Step Analysis Methods

In order to route dam failure magnitude flood flows within the TREX model a time step must be determined which is suitably small as to establish model numerical stability. The explicit scheme, finite difference numerical solving method employed by TREX will remain stable as long as a suitably short time step is used for the model calculations. TREX has a time step mode in which the model calculates the maximum time step allowed at every iteration that maintains numerical stability. This mode determines a time step which satisfies the Courant-Friedrichs-Lewy (CFL) condition.

\[
\frac{cdt}{dx} \leq C \tag{5.1}
\]

In Equation 5.1: 
- \(c\) = wave celerity 
- \(dt\) = model time step 
- \(dx\) = modeled raster cell size 
- \(C\) = Courant number

A finite differencing numerical model scheme has a physical domain of dependence which consists of a spatial dimension and a temporal dimension. The domain of dependence within a numerical model is the set of all points in the past from which information can propagate at or slower than the wave celerity (Julien 2002). The differencing domain, or numerical domain of dependence, consists of the set of state variable values used to determine the value of the next numerical solution. In order for a
forward marching numerical scheme to be stable, the numerical domain must be wider in the spatial dimension than the domain of dependence.

The Courant number can be thought of as the ratio of physical wave celerity to grid celerity. The Courant number effectively limits the total distance that wave energy can travel within every cell of a simulated domain to a percentage of the cell size for a simulated flow.

When the CFL model option is used within TREX, a Courant number is specified by the user as input. The unique model output of a simulation using this option is a file report of the model determined maximum stable time steps for every iteration of the simulation. Point source hydrographs were introduced to the California Gulch Watershed of varying peak discharge magnitudes while using the CFL option in order to determine the maximum time step required to maintain numerical stability as a function of input discharge. Courant
numbers of 0.2, 0.5, 0.8 and 1.0 were used as constraints for four different groups of simulations. Triangular input hydrographs with peak discharges ranging from 1 m³/s to 50,000 m³/s were routed through the watershed to the outlet. The lowest value of the stable time steps for each simulation was recorded. In this way a graphical representation of the model's stability dependence upon peak discharge and Courant number was created.

As seen in Figure 5.3, the stable time steps are sequentially reduced as Courant number is reduced. This result should be expected as the stable time step is directly proportional to the Courant number (Equation 5.1).

Figure 5.3: TREX, California Gulch point source stability
Also celerity should be expected to increase with increasing discharge as it is directly proportional to velocity (Equation 5.7). The stable time step also decreases as a power function of discharge.

A flood wave discharge can be approximated by an unsteady, one-dimensional flow in a wide rectangular impervious channel. The unit discharge \(q\), and flow velocity \(V\) can be approximated by a power functions of depth (Julien 2012).

\[
q = \alpha h^\beta \quad \text{(5.2)}
\]

\[
V = \alpha h^{\beta-1} \quad \text{(5.3)}
\]

Therefore, using the Manning coefficients for channel roughness,

\[
V = \alpha \left( \frac{q}{\alpha} \right)^{\left( \frac{\beta-1}{\beta} \right)} = \alpha^{0.6} q^{0.4} = \left( \frac{S_0}{n^{0.6}} \right)^{0.3} q^{0.4} \quad \text{(5.4)}
\]

In Equation 5.4: \(\alpha = \frac{S_0^{1/2}}{n}\) = Manning resistance coefficient for flow in the downstream direction

\(\beta= 5/3\) = Manning resistance exponent

\(q\) = Unit discharge

\(V\) = flow velocity

\(h\) = flow depth

\(S_0\) = Bed slope

\(n\) = Manning roughness coefficient

The Kleitz-Seddon relationship for floodwave celerity is the following (Julien 2012):

\[
c = \frac{\partial Q}{\partial A} \quad \text{(5.5)}
\]

The floodwave celerity equation then reduces to the following (Julien 2012):
\[
\frac{\partial h}{\partial t} + c \frac{\partial h}{\partial x} = 0
\]  \hspace{1cm} (5.6)

\[
c = \frac{\partial q}{\partial h} = \beta \alpha h^{\beta-1} = \beta V = \frac{5(S_0)^{0.3}}{3n^{0.6}} q^{0.4}
\]  \hspace{1cm} (5.7)

When this equation for celerity is inserted into the CFL equation, the following relationship between stable time step and discharge is obtained.

\[
dt \leq \left[ \frac{3C(dx)n^{0.6}}{5(S_0)^{0.3}} \right] q^{-0.4}
\]  \hspace{1cm} (5.8)

In Equation 5.8:
- \( c \) = wave celerity
- \( dt \) = model time step
- \( dx \) = modeled raster cell size
- \( C \) = Courant number

Substituting in the relationship between total discharge \( (Q) \) and unit discharge \( (q) \),

\[
dt \leq \left[ \frac{3C(dx)n^{0.6}W^{0.4}}{5(S_0)^{0.3}} \right] Q^{-0.4}
\]  \hspace{1cm} (5.9)

In Equation 5.9:
- \( W \) = Channel width
- \( Q \) = total discharge

Equation 5.9 provides a general theoretical description of the dependence of stable model time steps upon discharge. This relationship is very generalized and simplified. Also for high discharge flood flows there is no easy way to determine or assume a value for either the width of the flow, or for the Manning roughness coefficient \( (n) \). For these reasons it is not possible to make a direct comparison between model simulated stable time steps and theoretical values. However, what is noteworthy here is that the power of \(-0.4\) by which the time step varies with discharge in Equation 5.9 is in decent agreement
with the powers yielded by the point source CFL simulations plotted in Figure 5.3. These powers ranged from; -0.44 for a Courant number of 0.2, to -0.56 for a Courant number of 1.0. This result provides some evidence of a general agreement between the shape of the theoretical time step dependence and the modeled dependence.

The TREX model has been applied to other watersheds for the purpose of modeling extreme precipitation and flood events. Time step and discharge data were compiled from TREX flood simulations in watersheds in Korea and in Malaysia to compare stable flood simulations from other watersheds with the simulation results from California Gulch. The Duksan Creek and Naerin Creek watershed simulations from Korea were used (Kim 2012). Also the Lui, Semenyih and Kota Tinggi watershed simulations from Peninsular Malaysia were used (Abdullah 2013). These 5 watersheds all have very different hydrologic characteristics. Watershed areas vary from 33 km$^2$ to 1,635 km$^2$. Also variables such as slope, land use, soil type and vegetative cover vary widely between these watersheds and between these watersheds and the California Gulch watershed.

High return period rainfall-runoff events, up to magnitudes as extreme as PMP and GMP, were modeled in these watersheds. These simulations yielded peak outlet discharges for several rainfall events as well as stable time steps for these simulations. These time steps were not calculated by the model to be the maximum stable time steps, however, in the interest of establishing the fastest possible model run times for these simulations an iterative trial and error process was used to find stable time steps that were as large as possible while maintaining model numerical stability. So, these time steps can be assumed to be relatively close to the maximum stable time steps. These model setups incorporated a variety of spatial grid resolutions. They varied from 30m by 30m grid cell size to 230m
by 230m grid cell size. In order to compare all of these simulations and the simulations from California Gulch the model time step divided by the grid resolution was plotted against peak outlet discharge for each simulated event (Figure 5.4).

In Figure 5.4 a trend line was plotted for all of the rainfall-runoff simulations. Also the data from the California Gulch point source simulations with the Courant number of 1.0 was plotted. The trend line plotted for all of the watersheds proved to fit the data fairly well even given the wide range of modeled hydrologic variables between the different watersheds and different precipitation events. While the Courant trend line didn’t establish a boundary for the stable time steps, it did show general agreement with the multi-watershed data. Table 5.1 details the model input and output used for this analysis.
<table>
<thead>
<tr>
<th>Rainfall-Runoff Simulations Watershed Name</th>
<th>Watershed Area, A(km²)</th>
<th>Peak Outlet Discharge, Q(m³/s)</th>
<th>Precipitation Event Duration (hr)</th>
<th>[Rainfall Intensity(mm/hr), Time(hr)]</th>
<th>Grid Resolution, dx (m)</th>
<th>Time Step, dt (s)</th>
<th>dt/dx (s/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Duksan Creek</td>
<td>33</td>
<td>452</td>
<td>3</td>
<td>62</td>
<td>30</td>
<td>0.1</td>
<td>0.0033</td>
</tr>
<tr>
<td>Naerin Creek</td>
<td>1000</td>
<td>3300</td>
<td>3</td>
<td>76</td>
<td>180</td>
<td>0.1</td>
<td>0.0006</td>
</tr>
<tr>
<td>Lui</td>
<td>68</td>
<td>15</td>
<td>6</td>
<td>[(39.5, 1.0), (16.5, 2.0), (8.63, 0.0), (4.4, 4.0), (3.85, 0.0), (2.1, 6.0)]</td>
<td>90</td>
<td>1</td>
<td>0.0111</td>
</tr>
<tr>
<td>Lui</td>
<td>68</td>
<td>7</td>
<td>2</td>
<td>[(42.1, 1.0), (4.0, 2.0)]</td>
<td>90</td>
<td>1</td>
<td>0.0111</td>
</tr>
<tr>
<td>Semenyih</td>
<td>236</td>
<td>263</td>
<td>4</td>
<td>38</td>
<td>90</td>
<td>0.2</td>
<td>0.0022</td>
</tr>
<tr>
<td>Semenyih</td>
<td>236</td>
<td>1756</td>
<td>12</td>
<td>43.2</td>
<td>90</td>
<td>0.2</td>
<td>0.0022</td>
</tr>
<tr>
<td>Semenyih</td>
<td>1635</td>
<td>4527</td>
<td>10</td>
<td>85.7</td>
<td>90</td>
<td>0.1</td>
<td>0.0011</td>
</tr>
<tr>
<td>Kota Tinggi</td>
<td>1635</td>
<td>2820</td>
<td>168</td>
<td>7.6</td>
<td>230</td>
<td>0.5</td>
<td>0.0022</td>
</tr>
<tr>
<td>Kota Tinggi</td>
<td>1635</td>
<td>9664</td>
<td>120</td>
<td>25.8</td>
<td>230</td>
<td>0.1</td>
<td>0.0004</td>
</tr>
<tr>
<td>Kota Tinggi</td>
<td>1635</td>
<td>543</td>
<td>48</td>
<td>7</td>
<td>230</td>
<td>1</td>
<td>0.0043</td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>279</td>
<td>1</td>
<td>203</td>
<td>30</td>
<td>0.15</td>
<td>0.0050</td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>685</td>
<td>6</td>
<td>106</td>
<td>30</td>
<td>0.05</td>
<td>0.0017</td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>613</td>
<td>24</td>
<td>79</td>
<td>30</td>
<td>0.1</td>
<td>0.0033</td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>117</td>
<td>1</td>
<td>101</td>
<td>30</td>
<td>0.15</td>
<td>0.0050</td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>145</td>
<td>6</td>
<td>30</td>
<td>30</td>
<td>0.1</td>
<td>0.0033</td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>69</td>
<td>24</td>
<td>16</td>
<td>30</td>
<td>0.15</td>
<td>0.0050</td>
</tr>
<tr>
<td>Point Source Simulations Watershed Name</td>
<td>Watershed Area, A(km²)</td>
<td>Peak Input Discharge, Q (m³/s)</td>
<td>Grid Resolution, dx (m)</td>
<td>Time Step, dt (s)</td>
<td>dt/dx</td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>1</td>
<td>30</td>
<td>0.1000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>5</td>
<td>30</td>
<td>0.0300</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>10</td>
<td>30</td>
<td>0.0200</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>50</td>
<td>30</td>
<td>0.0100</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>500</td>
<td>30</td>
<td>0.0033</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>5000</td>
<td>30</td>
<td>0.0007</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>10000</td>
<td>30</td>
<td>0.0003</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>California Gulch</td>
<td>30</td>
<td>50000</td>
<td>30</td>
<td>0.0003</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Section 5.3 Empirical Relationships and Examples

While certainly limited, some data about dam breach flood flows has been collected over the past century. Most commonly the peak discharge may be known or be accurately estimated. Also the time to peak, or breach formation time, might be known. These data sets, while not forming a comprehensive picture of the dam breach outflow hydrograph, do lend some critical and useful information. The peak discharge from a dam breach can reveal much about the total extent of flooding downstream of a dam. The time to peak and breach formation time parameters can lend insight into early notification capabilities.

Peak discharge data has allowed researchers to empirically relate peak discharge data with various geometric parameters of dams. Some parameters that have been used in these types of regression analyses are: the maximum height of a dam, the depth of the water behind a dam, the volume of water behind a dam, and the crest length of a dam. Recently the results of many of the regression analyses that have been done over the past few decades were compiled for comparison and review (Thornton et al. 2011). These results can be found in Table 2.1 and Figure 2.2.

These empirical relationships can be incorporated into TREX simulations by using the model in conjunction with a GIS to determine the necessary parameter values for a certain precipitation event to create a dam breach outflow hydrograph, and then in turn inserting this hydrograph back into a simulation as a point source to be routed downstream.

The steps in this type of analysis are as follows:

1. Watershed input data must be collected, and the model must be calibrated and validated for the watershed of concern.
2. The dam of interest is constructed digitally in the Digital Elevation Model, DEM.

3. A precipitation event, the return period of which is of interest, is simulated on the new DEM.

4. The results of this simulation can be post processed in a GIS program to determine quantities such as the volume of water behind the dam at capacity. Also the simulation results can be used to determine the time to fill the reservoir.

5. Using one of the aforementioned empirical relationships, peak discharge and breach formation time can be estimated.

6. Using the estimated peak discharge, breach formation time, and breach initiation time, a triangular dam breach outflow hydrograph can be inserted into the model to simulate the dam breach flood.

7. This process can be repeated for any precipitation event and any type of dam or dam location.

This process could be used to analyze dam failures retrospectively or to create a set of failure scenario data for planning and forecasting pertaining to prospective dams. An example of this process was performed for the California Gulch site. The two hour duration, 100 year return period precipitation event was used as the input, and a 5 meter high earthen rectangular dam was used to create the reservoir. The volume of water stored behind the 5 meter high dam was calculated using a GIS. The empirical equation formulated by Pierce et al. 2010 was used to determine the peak discharge.

\[
Q_p = 0.038 (V_s^{0.475} H_d^{1.09})
\]

(5.10)

In Equation 5.10: \(V_s\) = volume of water stored behind the dam at capacity.
\( H_d = \text{height of the dam} \)

The empirical equation formulated by Froehlich 1995 was used for the time of failure.

\[
t_f = 0.00254 \left( V_s^{0.53} H_b^{0.90} \right)
\]

(5.11)

In Equation 5.11:

- \( V_s \) = volume of water stored behind the dam at capacity
- \( H_b \) = height of the water behind the dam

The time to initiation of the breach was determined from a simulation run which filled the reservoir. Assuming a triangular outflow hydrograph, which is most common, and a peak outflow occurring at the full formation of the breach, a hydrograph was created and input into TREX as a point source at the dam site during a simulation with precipitation. It was introduced to the simulation at the previously determined time at which overtopping began. This time was assumed to correspond to the time at which a breach formation would begin.

Figure 5.5 shows the results of the 100 year return period precipitation event simulation with the incorporated dam breach. Discharge was recorded and plotted for channel locations just downstream of the dam and at the outlet of the watershed.
Section 5.4  Areal Extent of Flood Plain Inundation

The areal extent of flooding due to a dam breach or large precipitation event has always been of interest in hydrologic engineering. The ability to estimate the areal extent of flooding near a stream can provide very useful information for structure design and floodplain property management. TREX has the ability to route flow into and out of the floodplain from the channel and to record gridded depths at a defined time interval. When the simulated output depths are input to a GIS program, the areal extent of flooding can be
visualized and quantified. The areal extent can be correlated to the return period of a storm or to the size of a dam failure.

Within a GIS program the model simulated depths up to a critical value can be displayed for any time step. This provides maps of the flooding up to a certain depth as the flood wave progresses downstream. This visualization could allow flood management programs to relate the areal extent of flood inundation with time. Additionally the total area inundated up to a critical value can be calculated to plot and analyze the magnitude of the areal extent of flooding relative to the size and timing of the input hydrograph.

Figures 5.6 through 5.8 show the results of a 4000 m$^3$/s peak discharge, one hour duration triangular input hydrograph as it is routed downstream. This point source was input to the model at the dam site described in Chapter VI and shown in Figure 6.2 and routed to the watershed outlet. These maps, which portray the flood plain area inundated to a depth of over 1 meter 45 minutes after the introduction of the flood wave to the watershed, were created in ESRI ARC Globe.
Figure 5.6: 4,000 m³/s point source floodplain inundation at 45 minutes after flood wave introduction, (depth ≥ 1 meter)
Figure 5.7: 4,000 m$^3$/s point source (zoom 1) floodplain inundation at 45 minutes after flood wave introduction, (depth ≥ 1 meter)
Figure 5.8: 4,000 m$^3$/s point source (zoom 2) floodplain inundation at 45 minutes after flood wave introduction, (depth ≥ 1 meter)
Through a GIS program the total flooded area downstream of an input point source can be calculated at every model time step. Figure 5.10 shows the total area flooded to a depth of over 1 meter downstream of the dam site for a 7,000 m³/s peak discharge input hydrograph.
**Section 5.5 Discussion of Results**

Point sources of varying magnitudes were input to the California Gulch watershed to determine the maximum permissible time step required to maintain numerical stability. The model stably routed flows of up to 50,000 m³/s peak discharge through the watershed. The CFL condition model time step option was employed to determine stable time steps given Courant numbers of 0.2, 0.5, 0.8, and 1.0. Simulations were run for a variety of peak discharge point source hydrographs and a plot was created showing the dependence of the...
stable model time step on peak discharge in California Gulch (Figure 5.3). These stability plots create a time step stability threshold for floodwave routing. The CFL simulations with a Courant number of 1.0 yielded the following trendline.

\[
dt = 2.35Q^{-0.56}, \quad C = 1.0 \tag{5.12}
\]

In order to compare this resultant time step stability condition with stable simulations from other watersheds, TREX rainfall-runoff simulation data were taken from 5 other watersheds. These data, along with stable simulation data from California Gulch, were plotted with the CFL stability threshold trendline with \( C = 1.0 \) (Figure 5.4). The rainfall-runoff simulations all had different grid resolutions, so in order to compile them onto one plot, the time step value of each simulation was divided by the grid cell size (\( dx \)) and plotted against peak outlet discharge.

A trend line was plotted for these data with an \( R^2 \) value of 0.81. This shows that there seems to be similarity across different watersheds between stable grid celerity and peak discharge. The CFL trend line did not create a boundary for all of the rainfall-runoff data. However the CFL power function had a similar power to that of the rainfall-runoff data and it appeared to plot through the centroid of the rainfall-runoff data fairly well. This function could be used as a first order estimation technique for determining stable model time steps for large scale and extreme rainfall runoff events and flood routing when a peak outlet discharge is known or can be estimated. If a peak outlet discharge is not known, a model simulation could be run using very conservative time steps in order to obtain a simulated peak outlet discharge. This peak outlet discharge could then be inserted in to the stable time step function to obtain a stable time step that is close to the threshold for
stability, and could be used for a series simulations. These methods could streamline the process of stable time step selection and reduce simulation run times which can be quite long for extreme events.

An example dam breach simulation was performed in the California Gulch watershed to demonstrate the ability of the TREX model to simulate dam failure events. An artificial dam was created within the California Gulch watershed and the 100 year return period magnitude storm was simulated. The volume of the reservoir and the time required to fill it were determined by a simulation with the reservoir initially empty. These values along with the input geometry of the artificial dam were input into empirical equations to determine the magnitude and timing of a simulated dam breach outflow hydrograph. This created hydrograph was then input into a simulation of the 100 year event to simulate the scenario wherein an empty reservoir fills completely and then fails due to overtopping.

The discharge was gaged just below the dam and at the outlet of the watershed to analyze the attenuation and lag of the flood wave. As expected, the hydrographs both downstream of the dam and at the outlet had sharper rising limbs and a greater peak discharge for the dam breach scenario than with no dam in place. Just downstream of the dam, the discharge was approximately 48% greater with the dam failure than with no dam in place. At the outlet, the peak discharge was approximately 5% greater with the dam breach than with no dam in place. This example dam overtopping and breach simulation was done to formalize and structure a process for dam breach simulation within the TREX model framework. This process could be used as a tool to analyze the downstream effects of prospective dams or to assess the potential downstream hazards of existing dams.
A point source of 7,000 m$^3$/s was used to create floodplain inundation maps through the use of a geographic information system. GIS was also used to quantify the total area of the floodplain that was flooded to a depth of over 1 meter. These mapping techniques demonstrate the ability to enhance model output visualization and interpretation through the use of GIS.
Chapter VI. Overtopping Modeling

Section 6.1 Overview of Work

Flooding from the overtopping of dams due to extreme precipitation events was simulated in California Gulch. Artificial dams were created in the California Gulch watershed DEM by modifying the elevations of cells in an arrangement across the channel. 14 dams of different heights up to 29 meters (as measured from the thalweg of the channel to the crest of the dam), and of lengths up to 780 meters (as measured across the crest), were created. Probable maximum precipitation (PMP) events were simulated as were even more extreme (global maximum precipitation, GMP) events. The GMP events precipitation intensities were estimated from an empirical relationship of the world’s greatest measured precipitation events (Jennings 1950). Discharge was recorded in the channel just downstream of the dam and also at the outlet of the watershed in order to analyze the effect of dams, or empty reservoirs, on discharges within the watershed. Time series of water depths for each cell within the watershed were also recorded.

Section 6.2 Dam Possibilities and Locations

The method for constructing artificial dams within a watershed involves using a GIS program to locate the dam site and determine the raster cell elevation values within the DEM that should be modified to simulate the desired dam geometry across a channel. Any combination of raster cell elevations that can represent a digital dam can be created. Rectangular or triangular profile dams can be created. Spillways can be simulated by the dimensions of the channel through the dam crest cell or by lowering a cell along the crest of the dam. Figures 6.1 and 6.3 display examples of the dams simulated.
Dams of triangular and rectangular profile were created at a location within the California Gulch watershed for this analysis. Dam height was simulated from 1 meter to 29 meters as measured from the channel thalweg. A site was chosen within the California Gulch watershed which would be the most conducive to creating a variety of artificial digital dams within the watershed. The chosen location is on the main stem within the watershed, and just downstream of the city of Leadville.

The dam site shown in Figure 6.2 was used as the location for all of these simulations. The height of simulated dams was geographically restricted to no more than 29 meters. Any dam taller than 29 meters would be taller than the valley walls. This would force stored water out of the dammed valley at full reservoir capacity.
Figure 6.2: California Gulch artificial dam site location

Figure 6.3: Three-dimensional dam representation
Section 6.3  Effects of Dams on Outlet Hydrographs

6.3.1  Probable Maximum Precipitation Simulation Analysis Methods

PMP maps for the region of Colorado containing California Gulch were located and used to determine the magnitude of the precipitation intensities for the 1, 6, and 24 hour duration rainfall events (Appendix 1.0). These storms were then simulated within the California Gulch watershed with a variety of artificial dams in place. For all of the simulations presented here the rainfall was uniformly distributed over the watershed and the hyetographs were all rectangular starting and ending abruptly. Surface water within the watershed would collect in the empty reservoirs and in some cases overtop the dams, in which case a flood pulse would continue to the outlet of the watershed.
Figure 6.4: Overtopping simulation at: a) beginning of simulation, b) beginning of rainfall, c) completion of reservoir filling, d) beginning of overtopping, e) peak of overtopping flow, f) flood recession
Figure 6.5: Example model output (6 hour duration GMP precipitation event dam overtopping simulation)
The 1 hour duration PMP intensity was found to be 101 mm/hr as determined through the PMP reports attained from the National Oceanographic and Atmospheric Administration (NOAA). Simulations were done with rectangular dams in place of heights: 5m, 7m, 9m, 12m, 15m, and 18m as measured from the thalweg of the channel. Also a simulation with no dam in place was done for comparison. Figure 6.6 shows the 1 hour duration PMP storm simulations for the dam site in California Gulch. A plot was also made that relates the peak outlet discharge to the height of the dams that were simulated.

Figure 6.8 shows the 6 hour duration PMP storm simulations for the dam site in California Gulch. The 6 hour duration PMP intensity was found to be 30 mm/hr also as determined from the NOAA PMP reports. Simulations were done with rectangular dams in place of heights: 5m, 7m, 9m, 12m, 15m, 18m, and 20m as measured from the thalweg of the channel and a simulation with no dam in place was done for comparison.

Finally, the 24 hour duration PMP storm event was simulated over the watershed (Figure 6.10). The 24 hour duration PMP intensity was determined to be 16 mm/hr. This precipitation intensity was simulated over the watershed with dams of heights 15m, 18m, 20m, 21m, 23m, 26m, and 29m in place. Plots were once again created of all the simulated outlet hydrographs and a plot of peak outlet discharge vs. dam height was created.
Figure 6.6: 1 hour duration PMP outlet discharge

Figure 6.7: 1 hour duration PMP peak outlet discharge vs. dam height
Figure 6.8: 6 hour duration PMP outlet discharge

Figure 6.9: 6 hour duration PMP peak outlet discharge vs. dam height
Figure 6.10: 24 hour duration PMP outlet discharge

Figure 6.11: 24 hour duration PMP peak outlet discharge vs. dam height
The families of curves shown in figures 6.6, 6.8, and 6.10 represent the full range of possible outlet discharge attenuations due to dams inserted at the dam site for the 1, 6, and 24 hour duration PMP simulations respectively. The maximum attenuation of the peak discharge at the outlet of the watershed was 63% for the 18 meter rectangular dam for the 1 hour duration PMP event. The maximum attenuation of the peak outlet discharge was 58% for the 6 hour duration PMP event with the 20 meter dam in place. The maximum attenuation of the peak outlet discharge was 46% for the 24 hour duration PMP event with the 29 meter dam in place. These results are summarized in Table 6.1.

Table 6.1: Summary of PMP simulation results

<table>
<thead>
<tr>
<th>PMP Event Duration</th>
<th>Precipitation Intensity (mm/hr)</th>
<th>Peak Outlet Discharge Without Dam (m³/s)</th>
<th>Height of Dam causing maximum attenuation of flood (m)</th>
<th>Peak Outlet Discharge With Dam (m³/s)</th>
<th>Attenuation (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 hour</td>
<td>101</td>
<td>117</td>
<td>18</td>
<td>43</td>
<td>63</td>
</tr>
<tr>
<td>6 hour</td>
<td>30</td>
<td>145</td>
<td>20</td>
<td>61</td>
<td>58</td>
</tr>
<tr>
<td>24 hour</td>
<td>16</td>
<td>69</td>
<td>26</td>
<td>38</td>
<td>46</td>
</tr>
</tbody>
</table>

6.3.2 Global Maximum Precipitation Simulation Analysis Methods

A similar analysis to the previously described PMP analysis was done with precipitation intensities derived from a compilation of the world’s largest measured precipitation events or global maximum precipitation (GMP) events (Jennings 1950). Precipitation intensities for the 1, 6, and 24 hour duration GMP events were derived from the plot in Figure 6.12 and used as TREX model input in order to quantify flood wave attenuation at the outlet of California Gulch due to dams of various crest heights. The
simulated hyetographs were rectangular and the rainfall was uniformly distributed over the watershed.

Figure 6.12: World's greatest measured precipitation

Figure 6.13 shows the family of curves describing the possible outlet flood wave attenuation due to dams when the 1 hour duration, 203 mm/hr intensity GMP event is introduced to the watershed. Dams of heights 7m, 9m, 12m, 15m, 18m, 20m, 21m, 23m, and 26m were introduced to the watershed.

A 23 meter high dam achieved the maximum flood wave attenuation of 59 %. Discharge was also plotted versus dam height for this event for a better interpretation of the dependence of peak outlet discharge on dam height. This same analysis technique was done for the 6 hour duration GMP event (Figure 6.15). A precipitation intensity of 106 mm/hr was used. Dams of heights 12m, 18m, 21m, 23m, 26m, and 29m were introduced to
the watershed. With the 29 meter high maximum height dam in place, overtopping began at approximately hour 4 and the flood wave reached the outlet in just under 1 hour. The maximum attenuation of the outlet discharge from the 6 hour duration event was determined to be 21%. This was accomplished by the 29 meter high dam. Finally, the 24 hour duration GMP event was simulated (Figure 6.17). A rainfall intensity of 79 mm/hr was simulated over the watershed and dams of heights 18m, 21m, 23m, 26m, and 29m were introduced to the dam site. The maximum attenuation of the outlet discharge for the 24 hour GMP event was determined to be 9%. This was the attenuation due to the 29m dam. Table 6.2 is a compilation of all of the GMP results.
Figure 6.13: 1 hour duration GMP outlet discharge

Figure 6.14: 1 hour duration GMP peak outlet discharge vs. dam height
Figure 6.15: 6 hour duration GMP outlet discharge

Figure 6.16: 6 hour duration GMP peak outlet discharge vs. dam height
Figure 6.17: 24 hour duration GMP outlet discharge

Figure 6.18: 24 hour duration GMP peak outlet discharge vs. dam height
Table 6.2: Summary of GMP simulation results

<table>
<thead>
<tr>
<th>GMP Event Duration</th>
<th>Precipitation Intensity (mm/hr)</th>
<th>Peak Outlet Discharge Without Dam (m³/s)</th>
<th>Height of Dam causing maximum attenuation of flood (m)</th>
<th>Peak Outlet Discharge With Dam (m³/s)</th>
<th>Attenuation (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 hour</td>
<td>203</td>
<td>279</td>
<td>23</td>
<td>115</td>
<td>59</td>
</tr>
<tr>
<td>6 hour</td>
<td>106</td>
<td>685</td>
<td>29</td>
<td>545</td>
<td>21</td>
</tr>
<tr>
<td>24 hour</td>
<td>79</td>
<td>613</td>
<td>29</td>
<td>557</td>
<td>9</td>
</tr>
</tbody>
</table>

Section 6.4 Discussion of Results

The estimated PMP and GMP events of duration 1, 6, and 24 hours were simulated in the California Gulch watershed. The precipitation was modeled as uniformly distributed over the watershed. The simulated hyetographs were rectangular. Simulations with these precipitation intensities were incorporated with artificial rectangular shaped dams inserted across the main stem channel in California Gulch. The height of these dams ranged from 5 meters to 29 meters as measured from the thalweg of the channel and the width of all of the dams was 30 meters. The created reservoirs were modeled as initially empty, and the initial soil moisture condition was modeled as dry (no recent precipitation). The process of filling the reservoir resulted in attenuation of the outlet hydrograph relative to the outlet hydrograph produced without an upstream reservoir. In some cases the dam was overtopped and a flood pulse was routed through the downstream flood plain to the outlet of the watershed.

The magnitude of the attenuation of the outlet discharge was quantified for each precipitation event and plotted. The results of these simulations, including the maximum attenuation of the outlet hydrographs, are summarized in Tables 6.1 and 6.2. These series of simulations demonstrate and confirm the ability of TREX to model the backwater effect.
of dams within a watershed. A process was developed utilizing a GIS program for modifying the DEM of a watershed to represent simple dams across a channel within a watershed. This process can be transferred to other watersheds where dams are proposed or where changes in discharge due to an existing upstream dam are to be studied. This analytical technique will provide a process for estimating downstream flood wave attenuation which could be useful in the implementation of dams and channel conveyance structures downstream of dams.
Chapter VII. Conclusions

Section 7.1 Conclusions about TREX Overtopping Modeling and Flood Routing

Input point source hydrographs of peak discharge up to 50,000 m$^3$/s were stably routed through the California Gulch watershed showing that flows far surpassing realistic magnitudes can be simulated. Relationships were determined between simulated peak input discharges and stable time steps for Courant numbers between 0.2 and 1.0.

Stable time step and peak outlet discharge data were taken from several TREX rainfall-runoff simulations from other watersheds to compare with California Gulch data. The trend line determined for the multi-watershed rainfall-runoff data fit the data fairly well, implying that stable grid celerity as a function of flood discharge could be somewhat transferable between watersheds. Also this trend line was in relatively good agreement with the CFL trend line from the California Gulch point source simulations showing that point source flood routing can yield basic information about simulation time step stability that could be useful when applied to other types of flood simulations like rainfall-runoff.

The computer modeled routing of a hydrograph through a watershed can be a powerful tool for flood plain management and dam design. In many cases a two-dimensional model provides a more accurate simulation of the flood flow interaction with the flood plain than does a one-dimensional model. A watershed scale two-dimensional model such as TREX can be a very appropriate tool for routing known or modeled flood wave hydrographs through a watershed. The TREX model allows as input a specified hydrograph at a specified location within a watershed. Using this method within TREX to route a dam breach flood provides the benefits of two-dimensional flow inundation of the
floodplain. The distributed parameters within the model also allow for much detail in the characterization of the floodplain. Also, as large discharge event flow data is scarce, calibrating models for these types of events is difficult. A physically based model such as TREX that allows for high resolution detail of the input parameters could be a valid flow estimation tool for events occurring in areas with little or no flow data.

An example scenario was created to simulate the watershed scale effect of a dam breach through the use of the TREX model and empirical dam breach equations. This modeling technique utilizes existing dam failure data and the routing ability of the distributed parameter, two-dimensional TREX model to create simulations of the dam failure process at the watershed scale due to extreme precipitation events. This analysis technique could be useful in floodplain management and planning.

Areal flood mapping was done using TREX and the ESRI ARC suite of GIS tools to quantify the extent of floodplain inundation due to hypothetical flood conditions within the California Gulch watershed, and to exemplify enhanced visualization techniques of the flooding process. The areal distribution and timing of flood plain inundation due to the failure of a proposed or existing dam can be estimated and correlated to dam characteristics such as crest height or to precipitation intensity. Inversely, the crest height of a proposed dam which would be necessary to attenuate a flood wave to the point of not damaging existing infrastructure or buildings could be determined through this analysis technique.

The TREX watershed model successfully simulated large scale (PMP and GMP) precipitation events. The model also successfully simulated geometrically simple dams of a variety of sizes. The results of the simulated dam overtopping events were compiled to
quantify the effect that empty reservoirs can have on downstream discharge. The correlation between dam characteristics, such as crest height, and downstream discharge can be useful. This type of modeling could be quite beneficial as a first order estimation tool for the effectiveness of check dams in flood wave attenuation. If a downstream design maximum allowable discharge was known for a watershed, then the crest height of a dam at a selected location upstream which was necessary to attenuate a flood wave to the allowable discharge could be roughly determined. This analytical technique can be employed for a variety of precipitation events and could be used to correlate a new outlet discharge with storm return period. This technique could be used to help facilitate the processes of dam site location and building material estimation for a proposed dam. Inversely, downstream flooding effects due to the overtopping of an existing dam could be quantified.
References


Appendices

Appendix 1.0 Probable Maximum Precipitation Maps

Figure A1.1: 1 hour duration PMP map for California Gulch
(http://www.nws.noaa.gov/oh/hdsc/PMP_documents/HMR55A_Plates_I_III.pdf)
Figure A1.2: 6 hour duration PMP map for California Gulch
(http://www.nws.noaa.gov/oh/hdsc/PMP_documents/HMR55A_Plates_I_IIII.pdf)
Figure A1.3: 24 hour duration PMP map for California Gulch
(http://www.nws.noaa.gov/oh/hdsc/PMP_documents/HMR55A_Plates_I_III.pdf)
## Appendix 2.0  Comparison of Popular Hydrologic Models

Table A2.1: Hydrologic model inter-comparison (Singh et al. 2002)

<table>
<thead>
<tr>
<th>Model name/acronym</th>
<th>Author(s) (year)</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stanford watershed Model (SWM)/Hydrologic Simulation</td>
<td>Crawford and Linsley (1960),</td>
<td>Continuous, dynamic event or steady-state simulator of hydrologic and</td>
</tr>
<tr>
<td>Package-Fortran IV (ESPIF)</td>
<td>Ricknell et al. (1993)</td>
<td>hydraulic and water quality processes</td>
</tr>
<tr>
<td>Catchment Model (CM)</td>
<td>Dawson and O'Donnell (1965)</td>
<td>Lumped, event-based runoff model</td>
</tr>
<tr>
<td>Tennessee Valley Authority (TVA) Model</td>
<td>TVA, Valley Authority (1972)</td>
<td>Lumped, event-based runoff model</td>
</tr>
<tr>
<td>U.S. Department of Agriculture Hydrograph Laboratory (USDAR) Model</td>
<td>Holman and Lopez (1971),</td>
<td>Event-based, process-oriented,</td>
</tr>
<tr>
<td>U.S. Geological Survey (USGS) Model</td>
<td>Holman et al. (1974)</td>
<td>lumped hydrograph model</td>
</tr>
<tr>
<td>Utah State University (USU) Model</td>
<td>Dawson et al. (1970, 1978)</td>
<td>Process-oriented, continuous, event-based runoff model</td>
</tr>
<tr>
<td>Purdue Model</td>
<td>Andrews et al. (1973)</td>
<td>Process-oriented, event, continuous, event runoff model</td>
</tr>
<tr>
<td>Antecedent Precipitation Index (API) Model</td>
<td>Seimer et al. (1969)</td>
<td>Lumped, river flow forecast model</td>
</tr>
<tr>
<td>National Weather service-River Forecast System (NWS-RFS)</td>
<td>Burnath et al. (1973a,b), Burnath (1975)</td>
<td>Lumped, continuous river forecast system</td>
</tr>
<tr>
<td>University of British Columbia (UBC) Model</td>
<td>Quick and Pigno (1977, 1979)</td>
<td>Process-oriented, lumped parameter, continuous simulation model</td>
</tr>
<tr>
<td>Agricultural Runoff Model (ARM)</td>
<td>Doognan et al. (1977)</td>
<td>Process-oriented, lumped runoff simulation model</td>
</tr>
<tr>
<td>Great Lakes Environmental Research Laboratory (GLERL) Model</td>
<td>Croley (1982, 1983)</td>
<td>Lyned, event-based runoff model</td>
</tr>
<tr>
<td>Classics, Runoff, and Erosion from Agricultural Management Systems (CREAMS)</td>
<td>USDA (1980)</td>
<td>quality model</td>
</tr>
<tr>
<td>Areal Non-point Source Watershed Environment Response Simulation (ANSWERS)</td>
<td>Bentley et al. (1972), Bouchard et al. (2002)</td>
<td>Event-based or continuous, lumped parameter and sediment yield</td>
</tr>
<tr>
<td>Erosion Productivity Impact Calculator (EPIC) Model</td>
<td>Williams et al. (1984), Williams (1993a,b)</td>
<td>Process-oriented, lumped, parameter, continuous water quantity and</td>
</tr>
<tr>
<td>Simulator for Water Resources in Rural Basins (SWRB)</td>
<td>Williams et al. (1985), Williams (1993a,b)</td>
<td>quality simulation model</td>
</tr>
</tbody>
</table>
Table A2.2: Hydrologic model inter-comparison continued (Singh et al. 2002)

<table>
<thead>
<tr>
<th>Model name/acronym</th>
<th>Author(s) (year)</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>System Hydrological European/Système Hydrologique</td>
<td>Abbott et al. (1986)</td>
<td>Physically based, distributed, continuous streamflow and sediment simulation</td>
</tr>
<tr>
<td>European Sediment (SHE/SEHED)</td>
<td>Bathurst et al. (1995)</td>
<td></td>
</tr>
<tr>
<td>Institute of Hydrology Distributed Model (IHM)</td>
<td>Beven et al. (1987), Beven and Kirkby (1979)</td>
<td></td>
</tr>
<tr>
<td>Agricultural Non-Point Source Model (AGNPS)</td>
<td>Beven (1995)</td>
<td></td>
</tr>
<tr>
<td>Kinematic Runoff and Erosion Model (KINEROS)</td>
<td>Young et al. (1989, 1993)</td>
<td></td>
</tr>
<tr>
<td>Groundwater Loading Effects of Agricultural Management Systems (GLEAMS)</td>
<td>Woodruff et al. (1990), Smith et al. (1995)</td>
<td></td>
</tr>
<tr>
<td>Simple Lumped Reservoir Parameter (SLURP) Model</td>
<td>Kita (1995)</td>
<td></td>
</tr>
<tr>
<td>Snowmelt Runoff Model (SRM)</td>
<td>Nava (1995)</td>
<td></td>
</tr>
<tr>
<td>THALES</td>
<td>Gupta et al. (1995)</td>
<td></td>
</tr>
<tr>
<td>Constrained Linear Simulation (CLS)</td>
<td>Natale and Todini (1971a, b)</td>
<td></td>
</tr>
<tr>
<td>ARNO (Reno River) Model</td>
<td>Todini (1985a, b)</td>
<td></td>
</tr>
<tr>
<td>Topographic Kinematic Approximation and Integration (TOPKAP) Model</td>
<td>Todini (1995)</td>
<td></td>
</tr>
<tr>
<td>Hydrological (GHUEM) Model</td>
<td>Morin et al. (1993, 1995)</td>
<td></td>
</tr>
<tr>
<td>Large Scale Catchment Model (LASCA)</td>
<td>Symplon et al. (1996a, b)</td>
<td></td>
</tr>
<tr>
<td>Rainfall–Runoff (R–R) Model</td>
<td>Kukkonen et al. (1999)</td>
<td></td>
</tr>
<tr>
<td>Soil–Vegetation–Atmosphere Transfer (SVAT) Model</td>
<td>Ma et al. (1999), Ma and Cheng (1998)</td>
<td></td>
</tr>
<tr>
<td>Hydrological Modeling System (ARE/ECMA)</td>
<td>Bedert and Plattner (1987), Lehner et al. (1999)</td>
<td></td>
</tr>
<tr>
<td>Macroscale Hydrological Model–Land Surface Scheme (MODUCOL-BSA)</td>
<td>Ledoux et al. (1989)</td>
<td></td>
</tr>
<tr>
<td>Regional-Scale Hydrologic Model (RHSM)</td>
<td>Nemer and Mohr (1996)</td>
<td></td>
</tr>
<tr>
<td>Global Hydrology Model (GHM0)</td>
<td>Kras et al. (1995)</td>
<td></td>
</tr>
<tr>
<td>System Hydrological European Transport (SHETRAN)</td>
<td>Wigmosta et al. (1994)</td>
<td></td>
</tr>
<tr>
<td>Cascade two dimensional Model (CASCADE)</td>
<td>Evett et al. (2000)</td>
<td></td>
</tr>
<tr>
<td>Surface Runoff, Infiltration, River Discharge and Groundwater Flow (SRIG)</td>
<td>Borah and Bera (2000), Borah et al. (1999)</td>
<td></td>
</tr>
</tbody>
</table>
Table A2.3: Hydrologic model inter-comparison continued (Singh et al. 2002)

<table>
<thead>
<tr>
<th>Model name/acroynm</th>
<th>Author(s) (year)</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modular Kinematic Model for Runoff Simulation (Modular System)</td>
<td>Stephenson (1989)</td>
<td>Physically based, lumped parameter, event-based runoff simulation model</td>
</tr>
<tr>
<td>Simplified Hydrology Model (SIMEHYD)</td>
<td>Wynn et al. (2002)</td>
<td></td>
</tr>
<tr>
<td>Stochastic Event Flood Model (SEFM)</td>
<td>Xu (1999)</td>
<td>Conceptual, lumped, continuous hydrologic model</td>
</tr>
<tr>
<td>Distributed Hydrological Model (HYDROTEL)</td>
<td>Georgakakos et al. (1999)</td>
<td>Process-oriented, distributed, rainfall and flow forecasting system</td>
</tr>
<tr>
<td>Agricultural Transport Model (ACTM0)</td>
<td>Scafe and Barker (1999)</td>
<td>Process-oriented, physically based event-based, flood simulation model</td>
</tr>
<tr>
<td>Soil Water Assessment Tool (SWAT)</td>
<td>Frey et al. (1975)</td>
<td>Physically based, distributed, continuous hydrologic simulation model</td>
</tr>
<tr>
<td></td>
<td>Arnold et al. (1998)</td>
<td>Lumped, conceptual, event-based runoff and water quality simulation model</td>
</tr>
</tbody>
</table>