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COMMENTS ON "BOUNDARY-LAYER TURBULENCE
MEASUREMENTS WITH MASS ADDITION AND COMBUSTION"

by

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ENGINEERING RESEARCH
AUG 20 '71
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COMMENTS ON "BOUNDARY - LAYER TURBULENCE MEASUREMENTS WITH MASS ADDITION AND COMBUSTION"

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In Reference (1) an investigation was made of the turbulent velocity fluctuation field in an isothermal boundary layer with homogeneous injection. The authors measured the shear stress distribution across the boundary layer and displayed the results in Fig. 5 of their paper as normalized shear stress as a function of velocity ratio ϕ .

In Reference (2) Meroney developed an analytical expression for the velocity profile across the turbulent transpired boundary layer together with an approximate technique to determine the normalized shear stress distribution. He proposed for a velocity profile near the wall

$$u^+ = y^+ + \frac{1}{2} (v_w^+) y^{+2} + \frac{1}{3!} (v_w^{+2}) y^{+3} + U_4^+ y^{+4} \quad (1)$$

and farther from the wall

$$u_\infty^+ - u^+ = \frac{v_w^+}{4k^2} \ln^2 \frac{y^+}{\delta^+} - \frac{1}{k} (1 + v_w^+ u_\infty^+)^{\frac{1}{2}} \ln \frac{y^+}{\delta^+} + \frac{\pi}{k} (1 + v_w^+ u_\infty^+)^{\frac{1}{2}} [2 - \omega(y^+/\delta^+)] \quad (2)$$

where the non-dimensional nomenclature have their conventional definitions, and the matching conditions have been computed to be

$$y_m^+ = 15.67 - 860 (v_w^+)^{\frac{1}{2}} / u_\infty^{+2} - 11.4 v_w^+ 0.45$$

$$U_y^+ = -5.4 \times 10^{-5} - 1.3 (v_w^+)^{1.7} / u_\infty^{+2} - 1.6 \times 10^{-2} v_w^{+1.7}$$

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The shear profile may be determined from the velocity profiles from

$$\frac{\tau}{\tau_w} \approx (1 + v_w^+ u^+) - (1 + v_w^+ u_\infty^+) \frac{2 \int_0^{y/\delta} (u^+)^2 d\xi - u^+ \int_0^{y/\delta} u^+ d\xi}{2 \int_0^1 (u^+)^2 d\xi - u_\infty^+ \int_0^1 u^+ d\xi} \quad (3)$$

Near the boundary Equation (3) reduces to

$$\frac{\tau}{\tau_w} \approx 1 + v_w^+ y^+ + \frac{v_w^{+2}}{2!} y^{+3} + v_w^+ U_4^+ y^{+4} \quad (4)$$

Figure 1 compares the calculated distributions of shear stress from Equations (1), (2) and (3) with the data displayed in Fig. 5 of Reference (1). The comparison is good except at very high blowing rates. Figure 2 compares measured values of the normalized maximum shear stress with computed values. Equation (3) seems to provide better agreement with this variation than a previously suggested correlation by Tennekes in Reference (3).

The rather large divergence of theory and data at high blowing rates in Fig. 1 may represent separation of the main flow from the transpired wall. If the flow parameters are compared with the somewhat limited criteria for attachment suggested by Hacker, this premise is strengthened. Hacker suggested an empirical blow-off criteria of

$$\frac{(\rho v)_w}{(\rho u)_\infty} Re^{1/5} = 0.08 \quad \text{for air into air transpiration at low Mach numbers.}$$

When the mass transfer number, B , equals twenty for the data in Reference (1), this expression equals approximately 0.11. In addition, the kink observed in the velocity profiles displayed as Fig. 2 of Reference (1) for $B = 20$ suggests the presence of separation.

REFERENCES

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FIGURE TITLES

Fig. 1 Shear stress distribution across the isothermal turbulent boundary

Fig. 2 Variation of pseudofriction velocity with mass transfer number

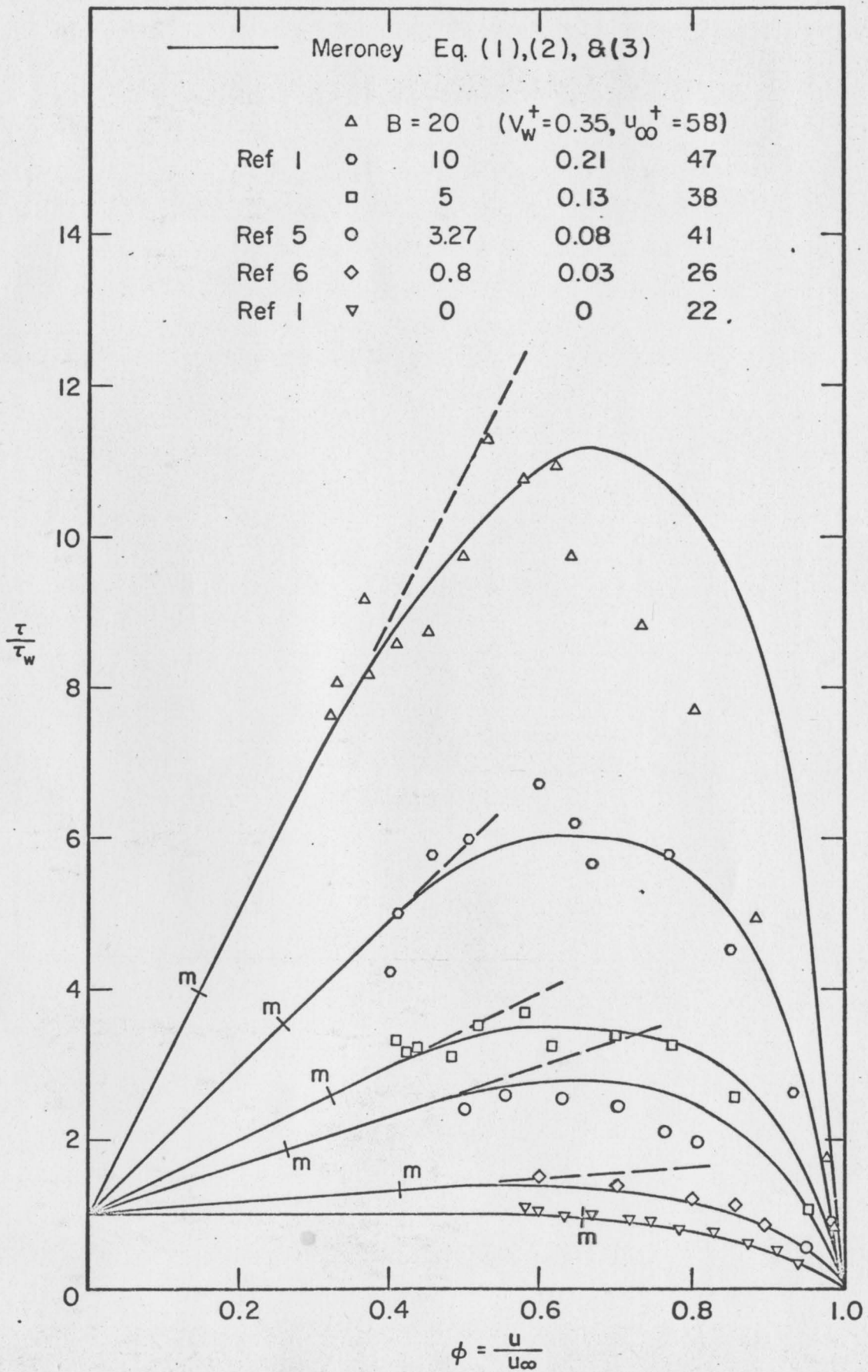


Fig 1

Shear stress distribution across the isothermal

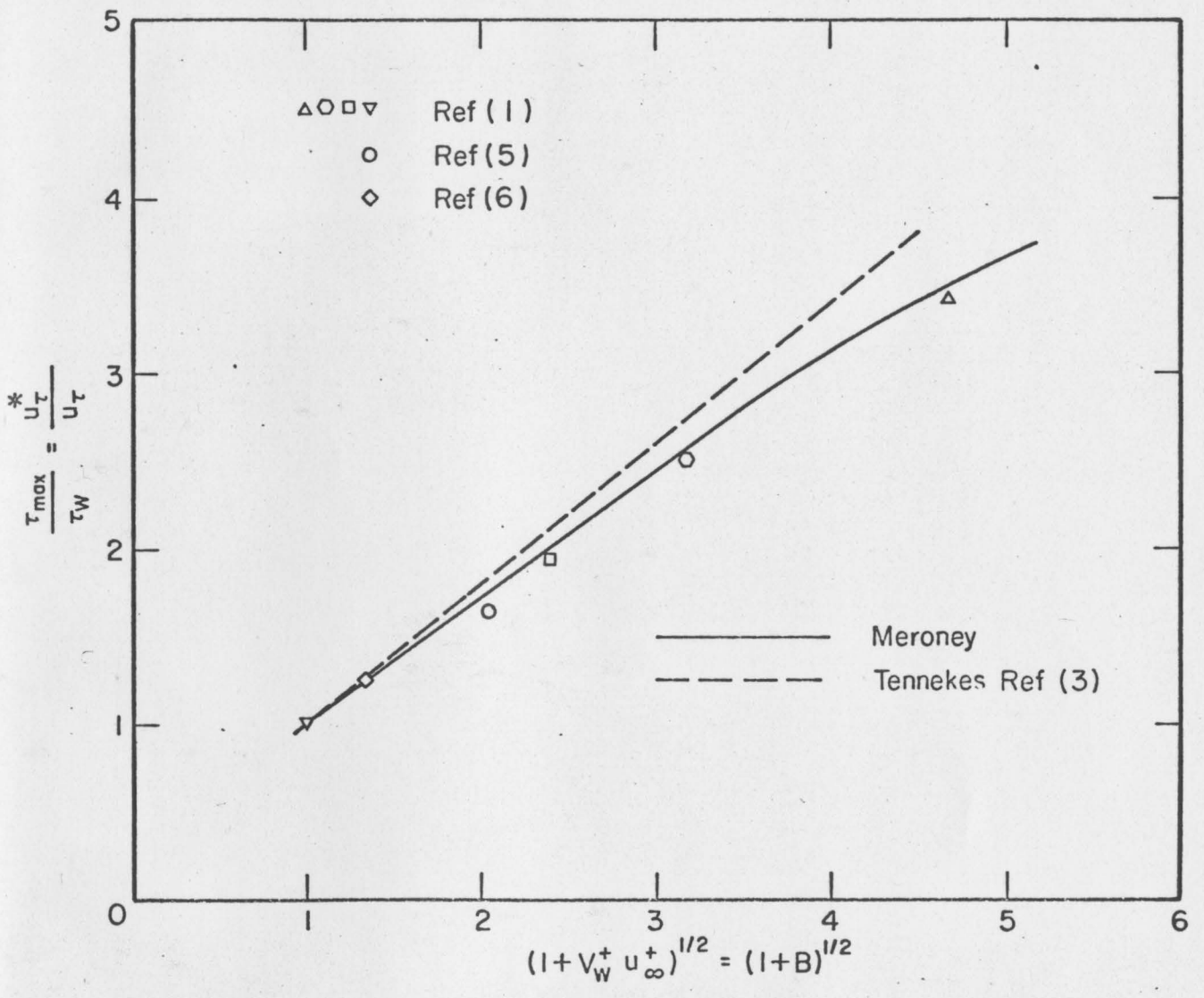


Fig 2

Variation of pseudo-fraction velocity with mass transfer number